

Question	Scheme	Marks	AOs
8(a)	Because $\frac{2}{\sqrt[3]{2-x}}$ is undefined at $x = 2$ and the limits of the integration are either side of this discontinuity	B1	2.4
		(1)	
(b)	$\int \frac{1}{\sqrt[3]{2-x}} dx = -3(2-x)^{\frac{2}{3}} (+c)$	M1 A1	2.1 1.1b
	$\int_0^5 \frac{2}{\sqrt[3]{2-x}} dx = \int_0^2 \frac{2}{\sqrt[3]{2-x}} dx + \int_2^5 \frac{2}{\sqrt[3]{2-x}} dx$	M1	3.1a
	$= \lim_{a \rightarrow 2^-} \int_0^a \frac{2}{\sqrt[3]{2-x}} dx + \lim_{b \rightarrow 2^+} \int_b^5 \frac{2}{\sqrt[3]{2-x}} dx$ $= \lim_{a \rightarrow 2^-} \left[-3(2-x)^{\frac{2}{3}} \right]_0^a + \lim_{b \rightarrow 2^+} \left[-3(2-x)^{\frac{2}{3}} \right]_b^5$ $= -3 \left(\lim_{a \rightarrow 2^-} \left((2-a)^{\frac{2}{3}} - (2-0)^{\frac{2}{3}} \right) \right) + -3 \left(\lim_{b \rightarrow 2^+} \left((2-5)^{\frac{2}{3}} - (2-b)^{\frac{2}{3}} \right) \right)$	M1	2.1
	$= -3 \left(-2^{\frac{2}{3}} + (-3)^{\frac{2}{3}} \right) = -3 \left(\sqrt[3]{9} - \sqrt[3]{4} \right)$	A1	2.2a
		(5)	

(6 marks)

Notes

(a)
B1: A correct explanation why the integral is improper

(b)
M1: Integrates to obtain an expression of the form $k(2-x)^{\frac{2}{3}}$

A1: Correct integration

M1: Adopts the correct strategy of splitting the integral into two with limits $0 \rightarrow 2$ and $2 \rightarrow 5$

M1: Produces a rigorous argument that includes an upper limit for the first integral that approaches 2 from below and a lower limit for the second integral that starts from 2 from above

A1: Correct expression (allow exact equivalents)