

| Question | Scheme | | Marks | AOs |
|-------------|---|--|-------|------|
| 5(a) | $\sin y = x \Rightarrow \cos y \frac{dy}{dx} = 1$ | $\sin y = x \Rightarrow \frac{dx}{dy} = \cos y$ | M1 | 1.1b |
| | Use $\sin^2 y + \cos^2 y = 1 \Rightarrow \cos y = \sqrt{1 - \sin^2 y} \Rightarrow \sqrt{1 - x^2}$ | | M1 | 2.1 |
| | $\frac{dy}{dx} = \frac{1}{\sqrt{1-x^2}}$ * cso | | A1* | 1.1b |
| | | | (3) | |
| (b) | Using the answer to (a) $f'(x) = \frac{1}{\sqrt{1-e^{2x}}} \times \dots$ | Restart $\sin y = e^x \Rightarrow \cos y \frac{dy}{dx} = e^x$ | M1 | 3.1a |
| | $f'(x) = \frac{1}{\sqrt{1-e^{2x}}} \times e^x$ | $f'(x) = \frac{e^x}{\cos y}$ | A1 | 1.1b |
| | $e^x \neq 0$ (or $e^x > 0$) therefore, there are no stationary points Alternatively, $e^x = 0$ leading to $x = \ln 0$ which is impossible/undefined therefore there are no stationary points. | | A1 | 2.4 |
| | | | (3) | |

(6 marks)

Notes:

(a)

M1: Finds x in terms of y and differentiates

M1: Uses the trig identity $\sin^2 y + \cos^2 y = 1$ to express $\cos y$ in terms of x . This may be seen in their derivative or stated on the side

A1*: Correctly achieves the printed answer $\frac{dy}{dx} = \frac{1}{\sqrt{1-x^2}}$. cso

(b)

M1: Differentiates using the chain rule to achieve the correct form, condone $f'(x) = \frac{1}{\sqrt{1-e^{2x}}}$

Note $f'(x) = \frac{1}{\sqrt{1-e^x}}$ is B0 for incorrect form

Alternatively restart, finds x in terms of y and differentiates

A1: Correct differentiation

A1: Follows correct differentiation. States that as $e^x \neq 0$ (or $e^x > 0$) or no solutions to $e^x = 0$ therefore there are no stationary points.

Alternatively, $e^x = 0$ leading to $x = \ln 0$ which is impossible/undefined/error therefore there are no stationary points. Ignore any reference to the denominator = 0