Question	Scheme		Marks	AOs
4(a)	$O \xrightarrow{3+\sqrt{5}}$ Initial line	Recalls correct shape for the type of curve.	B1	1.2
		Correct position with labelling of pole, initial line and point.	B1	1.1b
			(2)	
(b)	$\frac{\mathrm{d}}{\mathrm{d}\theta}(r\sin\theta) = \frac{\mathrm{d}}{\mathrm{d}\theta}(3\sin\theta + \sqrt{5}\sin\theta\cos\theta) = A\cos\theta + B\cos2\theta  \text{(oe)}$		M1	1.1b
	$\frac{\mathrm{d}}{\mathrm{d}\theta}(r\sin\theta) = \frac{\mathrm{d}}{\mathrm{d}\theta}(3\sin\theta + \sqrt{5}\sin\theta\cos\theta) = 3\cos\theta + \sqrt{5}\cos2\theta \text{ (oe)}$			1.1b
	$\frac{dy}{dx} = 0 \Rightarrow 3\cos\theta + \sqrt{5}\left(2\cos^2\theta - 1\right) = 0 \Rightarrow 2\sqrt{5}\cos^2\theta + 3\cos\theta - \sqrt{5} = 0$ $\Rightarrow \cos\theta = \frac{-3\pm\sqrt{9-4\left(2\sqrt{5}\right)\left(-\sqrt{5}\right)}}{4\sqrt{5}} = \dots$		M1	3.1a
	$\cos\theta = \frac{-3\pm7}{4\sqrt{5}}$ , quadrant 1 needs $\cos\theta > 0$ so $\cos\theta = \frac{1}{\sqrt{5}}$		A1	2.3
			(4)	
(c)	r=4		B1	1.1b
			(1)	
			(7 marks)	
Notes:				
(a) B1: Recalls the correct cardioid shape for this type of polar curve. B1: Correctly placed with the pole, initial line and point where curve crosses the initial line all indicated in some way.  (b) M1: Uses $y = r \sin \theta$ with the curve and attempts to differentiate. Accept any correct form but may have slips in coefficients, so e.g. as shown or $A\cos\theta + B\cos^2\theta + C\sin^2\theta$ can score M1. A1: Correct differentiation. Accept equivalents, e.g. $3\cos\theta + \sqrt{5}\cos^2\theta - \sqrt{5}\sin^2\theta$ M1: Sets their derivative equal to zero and attempts to find $\cos\theta$ (allow if $r\cos\theta$ was used) A1: Selects the correct value for $\cos\theta$ . If the other value is given it is A0 unless clearly rejected.  (c)				

**B1:** Correct value for *r*