

Question	Scheme	Marks	AOs
9	Gradient of chord = $\frac{(2(x+h)^3 + 5) - (2x^3 + 5)}{x+h-h}$	B1	1.1b
		M1	2.1
	$(x+h)^3 = x^3 + 3x^2h + 3xh^2 + h^3$	B1	1.1b
	Gradient of chord = $\frac{(2(x^3 + 3x^2h + 3xh^2 + h^3) + 5) - (2x^3 + 5)}{1+h-1}$		
	= $\frac{2x^3 + 6x^2h + 6xh^2 + 2h^3 + 5 - 2x^3 - 5}{1+h-1}$		
	= $\frac{6x^2h + 6xh^2 + 2h^3}{h}$		
	= $6x^2 + 6xh + 2h^2$	A1	1.1b
	$\frac{dy}{dx} = \lim_{h \rightarrow 0} (6x^2 + 6xh + 2h^2) = 6x^2$ and so at P, $\frac{dy}{dx} = 6(1)^2 = 6$	A1	2.2a
		(5)	
9 Alt 1	Let a point Q have x coordinate $1+h$, so $y_Q = 2(1+h)^3 + 5$	B1	1.1b
	$\{P(1, 7), Q(1+h, 2(1+h)^3 + 5)\} \Rightarrow$		
	Gradient PQ = $\frac{2(1+h)^3 + 5 - 7}{1+h-1}$	M1	2.1
	$(1+h)^3 = 1 + 3h + 3h^2 + h^3$	B1	1.1b
	Gradient PQ = $\frac{2(1 + 3h + 3h^2 + h^3) + 5 - 7}{1+h-1}$		
	= $\frac{2 + 6h + 6h^2 + 2h^3 + 5 - 7}{1+h-1}$		
	= $\frac{6h + 6h^2 + 2h^3}{h}$		
	= $6 + 6h + 2h^2$	A1	1.1b
	$\frac{dy}{dx} = \lim_{h \rightarrow 0} (6 + 6h + 2h^2) = 6$	A1	2.2a
	(5)		
(5 marks)			

Question 9 Notes:

B1: $2(x + h)^3 + 5$, seen or implied

M1: Begins the proof by attempting to write the gradient of the chord in terms of x and h

B1: $(x + h)^3 \rightarrow x^3 + 3x^2h + 3xh^2 + h^3$, by expanding brackets or by using a correct binomial expansion

M1: Correct process to obtain the gradient of the chord as $\alpha x^2 + \beta xh + \gamma h^2$, $\alpha, \beta, \gamma \neq 0$

A1: Correctly shows that the gradient of the chord is $6x^2 + 6xh + 2h^2$ and applies a limiting argument to deduce when $y = 2x^3 + 5$, $\frac{dy}{dx} = 6x^2$. E.g. $\lim_{h \rightarrow 0} (6x^2 + 6xh + 2h^2) = 6x^2$. Finally, deduces that at the point P , $\frac{dy}{dx} = 6$.

Note: δx can be used in place of h

Alt 1

B1: Writes down the y coordinate of a point close to P .

E.g. For a point Q with $x = 1 + h$, $\{y_Q\} = 2(1 + h)^3 + 5$

M1: Begins the proof by attempting to write the gradient of the chord PQ in terms of h

B1: $(1 + h)^3 \rightarrow 1 + 3h + 3h^2 + h^3$, by expanding brackets or by using a correct binomial expansion

M1: Correct process to obtain the gradient of the chord PQ as $\alpha + \beta h + \gamma h^2$, $\alpha, \beta, \gamma \neq 0$

A1: Correctly shows that the gradient of PQ is $6 + 6h + 2h^2$ and applies a limiting argument to deduce that at the point P on $y = 2x^3 + 5$, $\frac{dy}{dx} = 6$. E.g. $\lim_{h \rightarrow 0} (6 + 6h + 2h^2) = 6$

Note: For Alt 1, δx can be used in place of h