

Question	Scheme	Marks	AOs
4 (a)	Attempts $f(3) =$ and $f(4) =$ where $f(x) = \pm(2\ln(8-x) - x)$	M1	2.1
	$f(3) = (2\ln(5) - x) = (+)0.22$ and $f(4) = (2\ln(4) - 4) = -1.23$ <u>Change of sign</u> and function <u>continuous</u> in interval $[3, 4] \Rightarrow$ <u>Root</u> *	A1*	2.4
		(2)	
(b)	For annotating the graph by drawing a cobweb diagram starting at $x_1 = 4$ It should have at least two spirals	M1	2.4
	Deduces that the iteration formula <b>can be used</b> to find an approximation for $\alpha$ because <b>the cobweb spirals inwards</b> for the cobweb diagram	A1	2.2a
		(2)	

(4 marks)

**Notes:**

(a)

**M1:** Attempts  $f(3) =$  and  $f(4) =$  where  $f(x) = \pm(2\ln(8-x) - x)$  or alternatively **compares**  $2\ln 5$  to 3 and  $2\ln 4$  to 4. This is not routine and cannot be scored by substituting 3 and 4 in both functions

**A1:** Both values (calculations) correct to at least 1 sf with correct explanation and conclusion. (See underlined statements)

When comparing terms, allow reasons to be  $2\ln 8 = 3.21 > 3$ ,  $2\ln 4 = 2.77 < 4$  or similar

(b)

**M1:** For an attempt at using a cobweb diagram. Look for 5 or more correct straight lines. It may not start at 4 but it must show an understanding of the method. **If there is no graph then it is M0 A0**

**A1:** For a correct attempt starting at 4 and deducing that the iteration **can be used** as the iterations **converge to the root**. You must state that it can be used with a suitable reason. Suitable reasons could be "it spirals inwards", "it gets closer to the root", "it converges"

