- 4. The curve with equation  $y = 2\ln(8 x)$  meets the line y = x at a single point,  $x = \alpha$ .
  - (a) Show that  $3 < \alpha < 4$

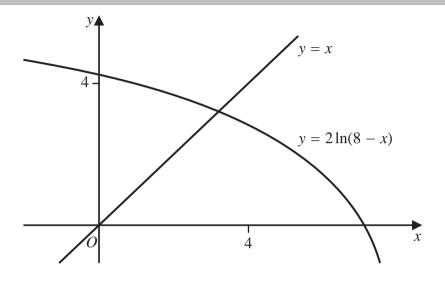


Figure 2

Figure 2 shows the graph of  $y = 2\ln(8 - x)$  and the graph of y = x.

A student uses the iteration formula

$$x_{n+1} = 2\ln(8 - x_n), \quad n \in \mathbb{N}$$

in an attempt to find an approximation for  $\alpha$ .

Using the graph and starting with  $x_1 = 4$ 

(b) determine whether or not this iteration formula can be used to find an approximation for  $\alpha$ , justifying your answer.

(2)