

Question	Scheme	Marks	AOs
9 (a)	$\frac{\sin x}{1 - \cos x} + \frac{1 - \cos x}{\sin x}$		
	$= \frac{\sin^2 x + (1 - \cos x)^2}{(1 - \cos x)\sin x}$	M1	2.1
	$= \frac{\sin^2 x + 1 - 2\cos x + \cos^2 x}{(1 - \cos x)\sin x}$	A1	1.1b
	$= \frac{1 + 1 - 2\cos x}{(1 - \cos x)\sin x}$	M1	1.1b
	$= \frac{2 - 2\cos x}{(1 - \cos x)\sin x} = \frac{2(1 - \cos x)}{(1 - \cos x)\sin x} = \frac{2}{\sin x} = 2\operatorname{cosec} x \quad \{k = 2\}$	A1	2.1
		(4)	
(b)	$\left\{ \frac{\sin x}{1 - \cos x} + \frac{1 - \cos x}{\sin x} = 1.6 \Rightarrow \right\} 2\operatorname{cosec} x = 1.6 \Rightarrow \operatorname{cosec} x = 0.8$ As $\operatorname{cosec} x$ is undefined for $-1 < \operatorname{cosec} x < 1$ then the given equation has no real solutions.	B1	2.4
		(1)	
(b) Alt 1	$\left\{ \frac{\sin x}{1 - \cos x} + \frac{1 - \cos x}{\sin x} = 1.6 \Rightarrow \right\} 2\operatorname{cosec} x = 1.6 \Rightarrow \sin x = 1.25$ As $\sin x$ is only defined for $-1 \leq \sin x \leq 1$ then the given equation has no real solutions.	B1	2.4
		(1)	

(5 marks)

Question 9 Notes:

(a) M1:	Begins proof by applying a complete method of rationalising the denominator
Note:	$\frac{\sin^2 x}{(1 - \cos x)\sin x} + \frac{(1 - \cos x)^2}{(1 - \cos x)\sin x}$ is a valid attempt at rationalising the denominator
A1:	Expands $(1 - \cos x)^2$ to give the correct result $\frac{\sin^2 x + 1 - 2\cos x + \cos^2 x}{(1 - \cos x)\sin x}$
M1:	Evidence of applying the identity $\sin^2 x + \cos^2 x \equiv 1$
A1:	Uses $\sin^2 x + \cos^2 x \equiv 1$ to show that $\frac{\sin x}{1 - \cos x} + \frac{1 - \cos x}{\sin x} \equiv 2\operatorname{cosec} x$ with no errors seen
(b) B1:	See scheme
(b) Alt 1 B1:	See scheme