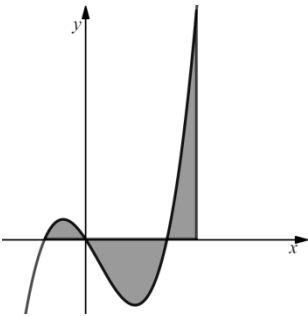


Question	Scheme	Marks	AOs
8 (a)	$y = x(x+2)(x-4) = x^3 - 2x^2 - 8x$	B1	1.1b
	$\int x^3 - 2x^2 - 8x \, dx \rightarrow \frac{1}{4}x^4 - \frac{2}{3}x^3 - 4x^2$	M1	1.1b
	Attempts area using the correct strategy $\int_{-2}^0 y \, dx$	dM1	2.2a
	$\left[\frac{1}{4}x^4 - \frac{2}{3}x^3 - 4x^2 \right]_{-2}^0 = (0) - \left(4 - \frac{-16}{3} - 16 \right) = \frac{20}{3} *$	A1*	2.1
		(4)	
(b)	For setting 'their' $\frac{1}{4}b^4 - \frac{2}{3}b^3 - 4b^2 = \pm \frac{20}{3}$	M1	1.1b
	For correctly deducing that $3b^4 - 8b^3 - 48b^2 + 80 = 0$	A1	2.2a
	Attempts to factorise $3b^4 - 8b^3 - 48b^2 \pm 80 = (b+2)(b+2)(3b^2 \dots b \dots 20)$	M1	1.1b
	Achieves $(b+2)^2(3b^2 - 20b + 20) = 0$ with no errors	A1*	2.1
		(4)	
(c)	 <p>States that between $x = -2$ and $x = 5.442$ the area above the x-axis = area below the x-axis</p>	B1	1.1b
		B1	2.4
		(2)	
(10 marks)			

(a)

B1: Expands $x(x+2)(x-4)$ to $x^3 - 2x^2 - 8x$ (They may be in a different order)**M1:** Correct attempt at integration of their cubic seen in at least two terms.Look for an expansion to a cubic and $x^n \rightarrow x^{n+1}$ seen at least twice**dM1:** For a correct strategy to find the area of R_1 It is dependent upon the previous M and requires a substitution of -2 into \pm their integrated function.The limit of 0 may not be seen. Condone $\left[\frac{1}{4}x^4 - \frac{2}{3}x^3 - 4x^2 \right]_{-2}^0 = \frac{20}{3}$ oe for this mark

A1*: For a rigorous argument leading to area of $R_1 = \frac{20}{3}$ For this to be awarded the integration must be correct

and the limits must be the correct way around and embedded or calculated values must be seen.

Eg. Look for $-\left(4 + \frac{16}{3} - 16\right)$ or $-\left(\frac{1}{4}(-2)^4 - \frac{2}{3}(-2)^3 - 4(-2)^2\right)$ or before you see the $\frac{20}{3}$

Note: It is possible to do this integration by parts.

(b)

M1: For setting their $\frac{1}{4}b^4 - \frac{2}{3}b^3 - 4b^2 = \pm \frac{20}{3}$ or $\left[\frac{1}{4}x^4 - \frac{2}{3}x^3 - 4x^2\right]_{-2}^b = 0$

A1: Deduces that $3b^4 - 8b^3 - 48b^2 + 80 = 0$. Terms may be in a different order but expect integer coefficients.

It must have followed $\frac{1}{4}b^4 - \frac{2}{3}b^3 - 4b^2 = -\frac{20}{3}$ or.

Do not award this mark for $\frac{1}{4}b^4 - \frac{2}{3}b^3 - 4b^2 + \frac{20}{3} = 0$ unless they attempt the second part of this question by expansion and then divide the resulting expanded expression by 12

M1: Attempts to factorise $3b^4 - 8b^3 - 48b^2 \pm 80 = (b+2)(b+2)(3b^2 \dots b \dots 20)$ via repeated division or inspection. FYI $3b^4 - 8b^3 - 48b^2 + 80 = (b+2)(3b^3 - 14b^2 - 20b + 40)$ Allow an attempt via inspection

$3b^4 - 8b^3 - 48b^2 \pm 80 = (b^2 + 4b + 4)(3b^2 \dots b \dots 20)$ but do not allow candidates to just write out

$3b^4 - 8b^3 - 48b^2 \pm 80 = (b+2)^2(3b^2 - 20b + 20)$ which is really just copying out the given answer.

Alternatively attempts to expand $(b+2)^2(3b^2 - 20b + 20)$ achieving terms of a quartic expression

A1*: Correctly reaches $(b+2)^2(3b^2 - 20b + 20) = 0$ with no errors and must have $= 0$

In the alternative obtains both equations in the same form **and states that they are same**. Allow \checkmark QED etc here.

(c) Please watch for candidates who answer this on Figure 2 which is fine

B1: Sketches the curve and a vertical line to the right of 4 ($x = 5.442$ may not be labelled.)

B1: Explains that (between $x = -2$ and $x = 5.442$) the area above the x -axis = area below the x -axis with appropriate areas shaded or labelled.

Alternatively states that the area between 1.225 and 4 is the same as the area between 4 and 5.442

Another correct statement is that the net area between 0 and 5.442 is $-\frac{20}{3}$

Look carefully at what is written. There are many correct statements/ deductions.

Eg. "(area between 0 and 4) - (area between 4 and 5.442) = $\frac{20}{3}$ ". Diagram below for your information.

