

| Question     | Scheme   | Marks    | AOs         |
|--------------|--|----------|-------------|
| <b>8 (a)</b> | (a) $P = (210, -5)$  | B1       | 1.1b        |
|              |  | B1       | 1.1b        |
|              |  | (2)      |             |
| <b>(b)</b>   | $5 \cos(x - 30^\circ) = 4 \sin x$  |          |             |
|              | Uses the compound angle identity and attempts to collect terms<br>$5 \cos x \cos 30^\circ + 5 \sin x \sin 30^\circ = 4 \sin x$<br>$5 \cos x \cos 30^\circ = \sin x(4 - 5 \sin 30^\circ)$ | M1       | 2.1         |
|              | Uses $\frac{\sin x}{\cos x} = \tan x$ $\tan x = \frac{5 \cos 30^\circ}{4 - 5 \sin 30^\circ} = \frac{5\sqrt{3}}{3}$ or awrt 2.89  | M1<br>A1 | 2.1<br>1.1b |
|              | $x = 70.9, 250.9$  | A1       | 1.1b        |
|              |  | (4)      |             |
| <b>(c)</b>   | Deduces the number of roots = 40   | B1ft     | 2.2a        |
|              | Offers a correct explanation. Eg States that there are <b>10</b> cycles of $360^\circ$ and $x \rightarrow 2x$ will mean that there are 4 roots between 0 and $360^\circ$ (not 2)         | B1       | 2.4         |
|              |  | (2)      |             |

(8 marks)

**Notes:**

(a)

**B1:** For one correct coordinate. Either  $P = (\dots, -5)$  or  $P = (210, \dots)$  but allow  $P = (210^\circ, \dots)$

**B1:** For  $P = (210, -5)$  but allow  $P = (210^\circ, -5)$

(b)

**M1:** Attempts to use the identity  $5 \cos(x - 30^\circ) \equiv 5 \cos x \cos 30^\circ + 5 \sin x \sin 30^\circ$  and attempts to collect terms. If the candidate divides by  $\cos x$  first then it is for collecting terms in  $\tan x$

**M1:** Divides by  $\cos x$ , uses the identity  $\tan x = \frac{\sin x}{\cos x}$  leading to  $\tan x = \dots$

**A1:**  $\tan x = \frac{5\sqrt{3}}{3}$  but allow  $\tan x = \text{awrt } 2.89$

**A1:** Both  $x = 70.9, 250.9$  (awrt 1dp) and no other answers. Allow  $x = 70.9^\circ, 250.9^\circ$

(c)

**B1ft:** Deduces that there will be 40 roots but follow through on  $20 \times$  the number of roots the candidate has between 0 and  $360^\circ$  in (b)

**B1:** Explains that  $3600^\circ$  is **10** cycles of  $360^\circ$  and  $x \rightarrow 2x$  will **double** the number roots between 0 and  $360^\circ$