

Question	Scheme	Marks	AOs
1 (a)	$(1+8x)^{\frac{1}{2}} = 1 + \frac{1}{2} \times 8x + \frac{\frac{1}{2} \times -\frac{1}{2}}{2!} \times (8x)^2 + \frac{\frac{1}{2} \times -\frac{1}{2} \times -\frac{3}{2}}{3!} \times (8x)^3$	M1 A1	1.1b 1.1b
	$= 1 + 4x - 8x^2 + 32x^3 + \dots$	A1	1.1b
		(3)	
(b)	Substitutes $x = \frac{1}{32}$ into $(1+8x)^{\frac{1}{2}}$ to give $\frac{\sqrt{5}}{2}$	M1	1.1b
	Explains that $x = \frac{1}{32}$ is substituted into $1 + 4x - 8x^2 + 32x^3$ and you multiply the result by 2	A1ft	2.4
		(2)	
<b>(5 marks)</b>			
<b>Notes:</b>			

(a)

**M1:** Attempts the binomial expansion with  $n = \frac{1}{2}$  and obtains the correct structure for term 3 **or** term 4.

Award for the correct coefficient with the correct power of  $x$ . Do not accept  ${}^n C_r$  notation for coefficients.

For example look for term 3 in the form  $\frac{\frac{1}{2} \times -\frac{1}{2}}{2!} \times (*x)^2$  or  $\frac{\frac{1}{2} \times -\frac{1}{2} \times -\frac{3}{2}}{3!} \times (*x)^3$

**A1:** Correct (unsimplified) expression. May be implied by correct simplified expression

**A1:**  $1 + 4x - 8x^2 + 32x^3$

Award if there are extra terms (even if incorrect).

Award if the terms are listed  $1, 4x, -8x^2, 32x^3$

(b)

**M1:** Score for substituting  $x = \frac{1}{32}$  into  $(1+8x)^{\frac{1}{2}}$  to obtain  $\frac{\sqrt{5}}{2}$  or equivalent such as  $\sqrt{\frac{5}{4}}$

Alternatively award for substituting  $x = \frac{1}{32}$  into **both sides** and making a connection between the two sides by use of an = or  $\approx$ .

E.g.  $\left(1 + \frac{8}{32}\right)^{\frac{1}{2}} = 1 + 4 \times \frac{1}{32} - 8 \times \left(\frac{1}{32}\right)^2 + 32 \times \left(\frac{1}{32}\right)^3$  following through on their expansion

Also implied by  $\frac{\sqrt{5}}{2} = \frac{1145}{1024}$  for a correct expansion

It is not enough to state substitute  $x = \frac{1}{32}$  into "the expansion" or just the rhs " $1 + 4x - 8x^2 + 32x^3$ "

**A1ft:** Requires a full (and correct) **explanation** as to how the expansion can be used to estimate  $\sqrt{5}$

E.g. Calculates  $1 + 4 \times \frac{1}{32} - 8 \times \left(\frac{1}{32}\right)^2 + 32 \times \left(\frac{1}{32}\right)^3$  and multiplies by 2.

This can be scored from an incorrect binomial expansion or a binomial expansion with more terms.

The explanation could be mathematical. So  $\frac{\sqrt{5}}{2} = \frac{1145}{1024} \rightarrow \sqrt{5} = \frac{1145}{512}$  is acceptable.

**SC:** For 1 mark, M1,A0 score for a statement such as "substitute  $x = \frac{1}{32}$  into both sides of part (a) and

make  $\sqrt{5}$  the subject"