

Question	Scheme	Marks	AOs
10(a)	$\frac{1 - \cos 2\theta + \sin 2\theta}{1 + \cos 2\theta + \sin 2\theta} = \frac{1 - (1 - 2\sin^2 \theta) + 2\sin \theta \cos \theta}{1 + \cos 2\theta + \sin 2\theta}$ <p style="text-align: center;">or</p> $\frac{1 - \cos 2\theta + \sin 2\theta}{1 + \cos 2\theta + \sin 2\theta} = \frac{1 - \cos 2\theta + \sin 2\theta}{1 + (2\cos^2 \theta - 1) + 2\sin \theta \cos \theta}$	M1	2.1
	$\frac{1 - \cos 2\theta + \sin 2\theta}{1 + \cos 2\theta + \sin 2\theta} = \frac{1 - (1 - 2\sin^2 \theta) + 2\sin \theta \cos \theta}{1 + (2\cos^2 \theta - 1) + 2\sin \theta \cos \theta}$	A1	1.1b
	$= \frac{2\sin^2 \theta + 2\sin \theta \cos \theta}{2\cos^2 \theta + 2\sin \theta \cos \theta} = \frac{2\sin \theta (\sin \theta + \cos \theta)}{2\cos \theta (\cos \theta + \sin \theta)}$	dM1	2.1
	$= \frac{\sin \theta}{\cos \theta} = \tan \theta^*$	A1*	1.1b
		(4)	
(b)	$\frac{1 - \cos 4x + \sin 4x}{1 + \cos 4x + \sin 4x} = 3\sin 2x \Rightarrow \tan 2x = 3\sin 2x \quad \text{o.e.}$	M1	3.1a
	$\Rightarrow \sin 2x - 3\sin 2x \cos 2x = 0$ $\Rightarrow \sin 2x(1 - 3\cos 2x) = 0$ $\Rightarrow (\sin 2x = 0,) \cos 2x = \frac{1}{3}$	A1	1.1b
	$x = 90^\circ, \text{ awrt } 35.3^\circ, \text{ awrt } 144.7^\circ$	A1 A1	1.1b 2.1
		(4)	
(8 marks)			
Notes			

(a)

M1: Attempts to use a correct double angle formulae for both  $\sin 2\theta$  and  $\cos 2\theta$  (seen once).

The application of the formula for  $\cos 2\theta$  must be the one that cancels out the "1"

So look for  $\cos 2\theta = 1 - 2\sin^2 \theta$  in the numerator or  $\cos 2\theta = 2\cos^2 \theta - 1$  in the denominator

Note that  $\cos 2\theta = \cos^2 \theta - \sin^2 \theta$  may be used as well as using  $\cos^2 \theta + \sin^2 \theta = 1$

A1:  $\frac{1 - (1 - 2\sin^2 \theta) + 2\sin \theta \cos \theta}{1 + (2\cos^2 \theta - 1) + 2\sin \theta \cos \theta}$  or  $\frac{2\sin^2 \theta + 2\sin \theta \cos \theta}{2\cos^2 \theta + 2\sin \theta \cos \theta}$

dM1: Factorises numerator and denominator in order to demonstrate cancelling of  $(\sin \theta + \cos \theta)$

A1\*: Fully correct proof with no errors.

You must see an intermediate line of  $\frac{2\sin \theta (\cancel{\sin \theta + \cos \theta})}{2\cos \theta (\cancel{\cos \theta + \sin \theta})}$  or  $\frac{\sin \theta}{\cos \theta}$  or even  $\frac{2\sin \theta}{2\cos \theta}$

Withhold this mark if you see, within the body of the proof,

- notational errors. E.g.  $\cos 2\theta = 1 - 2\sin^2$  or  $\cos \theta^2$  for  $\cos^2 \theta$
- mixed variables. E.g.  $\cos 2\theta = 2\cos^2 x - 1$

(b)

M1: Makes the connection with part (a) and writes the lhs as  $\tan 2x$ . Condone  $x \leftrightarrow \theta$   $\tan 2\theta = 3\sin 2\theta$

A1: Obtains  $\cos 2x = \frac{1}{3}$  o.e. with  $x \leftrightarrow \theta$ . You may see  $\sin^2 x = \frac{1}{3}$  or  $\cos^2 x = \frac{2}{3}$  after use of double angle formulae.

A1: Two "correct" values. Condone accuracy of awrt  $90^\circ$ ,  $35^\circ$ ,  $145^\circ$

Also condone radian values here. Look for 2 of awrt 0.62, 1.57, 2.53

A1: All correct (allow awrt) and no other values in range. Condone  $x \leftrightarrow \theta$  if used consistently

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Answers without working in (b): Just answers and no working score 0 marks.

If the first line is written out, i.e.  $\tan 2x = 3\sin 2x$  followed by all three correct answers score 1100.