

Question	Scheme	Marks	AOs
13	$(x-3)^2 + y^2 = \left(\frac{t^2+5}{t^2+1} - 3\right)^2 + \left(\frac{4t}{t^2+1}\right)^2$	M1	3.1a
	$= \frac{(2-2t^2)^2 + 16t^2}{(t^2+1)^2} = \frac{4+8t^2+4t^4}{(t^2+1)^2}$	dM1	1.1b
	$\frac{4(t^4+2t^2+1)}{(t^2+1)^2} = \frac{4(t^2+1)^2}{(t^2+1)^2} = 4^*$	A1*	2.1
		<b>(3)</b>	

M1: Attempts to substitute the given parametric forms into the Cartesian equation or the lhs of the Cartesian equation. There may have been an (incorrect) attempt to multiply out the  $(x-3)^2$  term

dM1: Attempts to combine (at least the lhs) using correct processing into a single fraction, multiplies out and collects terms on the numerator.

A1\*: Fully correct proof showing all key steps

Question	Scheme	Marks	AOs
Alt	$x = \frac{t^2+5}{t^2+1} \Rightarrow xt^2 + x = t^2 + 5 \Rightarrow t^2 = \frac{5-x}{x-1}$	M1	3.1a
	$y = \frac{4t}{t^2+1} \Rightarrow y^2 = \frac{16t^2}{(t^2+1)^2} = \frac{16\left(\frac{5-x}{x-1}\right)}{\left(\frac{5-x}{x-1} + 1\right)^2}$		
	$y^2 = \frac{16\left(\frac{5-x}{x-1}\right)}{\left(\frac{5-x}{x-1} + 1\right)^2} = 16\left(\frac{5-x}{x-1}\right) \times \left(\frac{(x-1)}{5-x+x-1}\right)^2 \Rightarrow y^2 = (5-x)(x-1)$	dM1	1.1b
	$y^2 = (5-x)(x-1) \Rightarrow y^2 = 6x - x^2 - 5$ $\Rightarrow y^2 = 4 - (x-3)^2 \text{ or other intermediate step}$ $\Rightarrow (x-3)^2 + y^2 = 4^*$	A1*	2.1
		<b>(3)</b>	

**(3 marks)**

**Notes**

M1: Adopts a correct strategy for eliminating  $t$  to obtain an equation in terms of  $x$  and  $y$  only. See scheme.

Other methods exist which also lead to an appropriate equation. E.g using  $t = \frac{y}{x-1}$

dM1: Uses correct processing to eliminate the fractions and start to simplify

A1\*: Fully correct proof showing all key steps