

Question	Scheme	Marks	AOs
8(a)	$\frac{1 - \cos 2\theta}{\sin^2 2\theta} = \frac{1 - (1 - 2\sin^2 \theta)}{\dots}$ or $\frac{1 - \cos 2\theta}{\sin^2 2\theta} = \frac{\dots}{(2\sin \theta \cos \theta)^2}$	M1	1.1b
	$\frac{1 - \cos 2\theta}{\sin^2 2\theta} = \frac{1 - (1 - 2\sin^2 \theta)}{(2\sin \theta \cos \theta)^2} = \frac{2\sin^2 \theta}{4\sin^2 \theta \cos^2 \theta} = \dots$	M1	2.1
	$= \frac{1}{2} \sec^2 \theta$	A1	1.1b
		(3)	
(b)	$\frac{1 - \cos 2x}{\sin^2 2x} = (1 + 2 \tan x)^2 \Rightarrow \frac{1}{2} \sec^2 x = 1 + 4 \tan x + 4 \tan^2 x$ $\Rightarrow 1 + \tan^2 x = 2 + 8 \tan x + 8 \tan^2 x \Rightarrow 7 \tan^2 x + 8 \tan x + 1 = 0$	M1	3.1a
	$\tan x = -1, -\frac{1}{7} \Rightarrow x = \dots$	M1	1.1b
	$x = -\frac{\pi}{4}, -0.142$	A1 A1	1.1b 1.1b
		(4)	

(7 marks)

Notes

(a)

M1: Applies $\cos 2\theta = 1 - 2\sin^2 \theta$ in the numerator or $\sin 2\theta = 2\sin \theta \cos \theta$ in the denominatorM1: Applies $\cos 2\theta = 1 - 2\sin^2 \theta$ in the numerator and $\sin 2\theta = 2\sin \theta \cos \theta$ in the denominator and simplifies to obtain $k \sec^2 \theta$

A1: Correct expression

(b)

M1: Makes the connection with part (a), squares the RHS, applies $\sec^2 x = 1 + \tan^2 x$ and collects terms to obtain a 3TQ in $\tan x$ M1: Solves a 3TQ in $\tan x$ and obtains at least 1 value for x A1: One correct value (allow -0.785 for $-\frac{\pi}{4}$)A1: Both correct and no other values in range (allow -0.785 for $-\frac{\pi}{4}$)