

Question	Scheme	Marks	AOs
14(i)	Let the consecutive odd integers be $2n - 1$ and $2n + 1$ $(2n - 1)^2 + (2n + 1)^2 = 4n^2 - 4n + 1 + 4n^2 + 4n + 1 = \dots$	M1	2.1
	$= 8n^2 + 2$	A1	1.1b
	So $(2n - 1)^2 + (2n + 1)^2$ is always 2 more than a multiple of 8	A1	2.4
		(3)	
(ii)	Assume that $\log_2 5$ is rational so that $\log_2 5 = \frac{a}{b}$ where $a$ and $b$ are integers	M1	2.4
	$\log_2 5 = \frac{a}{b} \Rightarrow 5 = 2^{\frac{a}{b}}$	M1	1.1b
	$5 = 2^{\frac{a}{b}} \Rightarrow 5^b = 2^a$	A1	2.2a
	This is a contradiction as a power of 2 cannot equal a power of 5 so $\log_2 5$ must be irrational	A1	2.4
		(4)	

(7 marks)

### Notes

(i)

M1: Starts the proof by stating 2 consecutive odd numbers, squares and adds and collects terms

A1: Correct expression

A1: Completes the proof with no errors and an appropriate conclusion

(ii)

M1: Begins the proof by negating the statement e.g.  $\log_2 5$  is rational

M1: Applies the definition of logs to eliminate the log

A1: Deduces that  $5^b = 2^a$

A1: A full and complete argument that completes the contradiction proof