

Question	Scheme	Marks	AOs
2	Sets $f(-2) = 0 \Rightarrow (-2-4)((-2)^2 - 3 \times -2 + k) - 42 = 0$	M1	3.1a
	$-6(k+10) = 42 \Rightarrow k = \dots$	M1	1.1b
	$k = -17$	A1	1.1b
		(3)	
			(3 marks)
Notes:			

M1: Attempts $f(-2) = 0$ leading to an equation in k . So $(-2-4)((-2)^2 - 3 \times -2 + k) - 42 = 0$ is fine

Condone slips but expect to see a first bracket of $(-2-4)$.

"- 42" must not be omitted but could appear as +42 with a sign slip.

There may have been attempts to expand $f(x) = (x-4)(x^2 - 3x + k) - 42$ before attempting to set $f(-2) = 0$. This is acceptable and condone slips/errors in the expansion, but the 42 must be present. FYI the expanded (and simplified) $f(x) = x^3 - 7x^2 + (12+k)x - 4k - 42$

M1: Solves a **linear** equation in k as a result of setting $f(\pm 2) = 0$.

The ± 42 must be there at some point when the substitution is made.

Allow minimal evidence here. A linear equation leading to a solution is fine.

If $f(x)$ is expanded then it is dependent upon being a cubic which contains a kx term and a '42'

A1: $k = -17$ correct answer following correct work but allow recovery from invisible brackets

Answers of $k = -17$ may appear with very little or no working, perhaps via trial and improvement.

If so, then marks can only be allocated if evidence is shown.

E.g. $k = -17 \Rightarrow f(x) = (x-4)(x^2 - 3x - 17) - 42$

$f(-2) = (-6) \times (-7) - 42 = 0$. Hence $(x+2)$ is a factor.

More difficult alternative methods may be seen

Alt I: You may see attempts via division / inspection

$$x+2 \overline{) \begin{array}{r} x^2 - 9x + (k+30) \\ x^3 - 7x^2 + (12+k)x - 4k - 42 \end{array}} \quad \text{Then sets remainder } -6k - 102 = 0 \Rightarrow k = -17$$

$$\underline{\underline{-6k - 102}}$$

M1: For dividing their cubic by $(x+2)$ which has both an x and a constant coefficient in k , leading to a quadratic quotient and a linear remainder in k which is then set = 0

M1: Solves a equation resulting from setting a linear remainder in k equal to 0 . It is dependent on the first M via this route

A1: Completely correct with $k = -17$

Alt II: You may also see a grid or an attempt at factorisation via inspection

	x^2	$-9x$	$-2k - 21$
x	x^3	$-9x^2$	$(-2k - 21)x$
$+2$	$2x^2$	$-18x$	$-4k - 42$

$$\text{OR } x^3 - 7x^2 + (12+k)x - 4k - 42 \equiv (x+2)(x^2 - 9x - 2k - 21)$$

which should be followed by equating the x terms to form an equation in k

$$12+k = -18 - 2k - 21 \Rightarrow 3k = -51 \Rightarrow k = -17$$

$$\text{OR } x^3 - 7x^2 + (12+k)x - 4k - 42 \equiv (x+2)(x^2 - 9x + k + 30)$$

which should be followed by equating the constant terms to form an equation in k

$$-4k - 42 = 2(k + 30) \Rightarrow 6k = -102 \Rightarrow k = -17$$

The above are examples. There may be other correct attempts so look at what is done.

M1: For an attempt at factorising E.g. $x^3 - 7x^2 + (12+k)x - 4k - 42 \equiv (x+2)(x^2 + bx + c)$ and attempting to set up three equations in b , c and k . E.g. $2+b = -7$, $2b+c = 12+k$, $2c = -4k - 42$

The expanded $f(x)$ must be a cubic which contains both a kx term and a '42'

M1: Solves the equations set up from an allowable equation to find k . It is dependent via this route.

A1: Completely correct with $k = -17$