

Question	Scheme	Marks	AOs
4 (a)	$\lim_{\delta x \rightarrow 0} \sum_{x=2.1}^{6.3} \frac{2}{x} \delta x = \int_{2.1}^{6.3} \frac{2}{x} dx$	B1	1.2
		(1)	
(b)	$= [2 \ln x]_{2.1}^{6.3} = 2 \ln 6.3 - 2 \ln 2.1$	M1	1.1b
	$= \ln 9 \quad \text{CSO}$	A1	1.1b
		(2)	
			(3 marks)
Notes:			

Mark (a) and (b) as one

(a)

B1: States that $\int_{2.1}^{6.3} \frac{2}{x} dx$ or equivalent such as $2 \int_{2.1}^{6.3} x^{-1} dx$ but must include the limits and the dx.

Condone $dx \leftrightarrow \delta x$ as it is very difficult to tell one from another sometimes

(b)

M1: Know that $\int \frac{1}{x} dx = \ln x$ and attempts to apply the limits (either way around)

Condone $\int \frac{2}{x} dx = p \ln x$ (including $p = 1$) or $\int \frac{2}{x} dx = p \ln qx$ as long as the limits are applied.

Also be aware that $\int \frac{2}{x} dx = \ln x^2$, $\int \frac{2}{x} dx = 2 \ln|x| + c$ and $\int \frac{2}{x} dx = 2 \ln cx$ o.e. are also correct

$[p \ln x]_{2.1}^{6.3} = p \ln 6.3 - p \ln 2.1$ is sufficient evidence to award this mark

A1: CSO $\ln 9$. Also answer $= \ln 3^2$ so $k = 9$ is fine. Condone $\ln|9|$

The method mark must have been awarded. Do not accept answers such as $\ln \frac{39.69}{4.41}$

Note that solutions appearing from "rounded" decimal work when taking lns should not score the final mark. It is a "show that" question

E.g. $[2 \ln x]_{2.1}^{6.3} = 2 \ln 6.3 - 2 \ln 2.1 = 2.197 = \ln k \Rightarrow k = e^{2.197} = 8.998 = 9$