| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 13(a) | $a=60$ | B1 | 3.1b |
|  | $2=$ " 60 " $-b(-20)^{2} \Rightarrow b=\ldots$ | M1 | 3.4 |
|  | $H=60-0.145(t-20)^{2}$ | A1 | 3.3 |
|  |  | (3) |  |
| (b) | Height $=2 \mathrm{~m}$ | B1 | 3.4 |
|  |  | (1) |  |
| (c) | $\alpha=180$ or $\beta=31$ | M1 | 3.4 |
|  | $H=29 \cos (9 t+180)^{\circ}+31$ | A1 | 3.3 |
|  |  | (2) |  |
| (d) | e.g. "The model allows for more than one circuit" | B1 | 3.5a |
|  |  | (1) |  |

## Notes

(a)

B 1: $a=60$ (may be seen in their final equation of the model or implied by 60 substituted for $a$ in the model)
M1: Attempts to find $b$ by substituting in $t=0, H=2$ and their $a$ and proceeding to a value for $b$.
May be seen as two simultaneous equations formed:
$2=a-b(-20)^{2}$ and $60=a-b(20-20)^{2}$ proceeding to a value for $b$
A1: $\quad H=60-0.145(t-20)^{2}$ or equivalent such as $H=-\frac{29}{200} t^{2}+5.8 t+2$ or $H=60-\frac{29}{200}(t-20)^{2}$ isw once a correct equation for the model is seen. Must be in terms of $H$ and $t$. If they just state $a=60, b=0.145$ then A0
A correct answer with no working seen scores full marks.
(b)

B1: 2 cao (condone lack of units) This can be scored even if their model in (a) is incorrect (they may have used symmetry to determine this value)
(c)

M1: $\quad(\alpha=) 180$ or $(\beta=) 31$ Condone $(\alpha=) \pi$
A1: $\quad H=29 \cos (9 t+180)^{\circ}+31$ or equivalent e.g. $H=-29 \cos (9 t)+31$ isw once a correct equation for the model is seen. Must be in terms of $H$ and $t$. If they just state $\alpha=180, \beta=31$ then A0.
A correct equation with no working seen scores both marks. Does not require the degree symbol.
(d)

B1: Score for a reason which makes reference to any of

- the alternative model allows repetition (allow phrases e.g. "multiple cycles", "repeated circuits", "cyclical", "periodic", "loops around", "the original model can only go up and down once")
- the alternative model after 2 minutes the carriage will be back at the start (e.g."at $2 \mathrm{mins}, H=2$ ")
- the original/quadratic model after 40 seconds (or any time after this) will be negative (e.g. "the height will be negative which cannot happen")
- the original model after 2 minutes would not be back at the start

Do not allow vague responses on their own e.g. "the original model is a parabola"
If calculations are used then they must be correct using a correct model (allow rounded or truncated) Look for a valid reason and ignore reference to anything else as long as it does not contradict

| $t$ | 0 | 5 | 10 | 15 | 20 | 25 | 30 | 35 | 40 | 45 | 50 | 55 | 60 | 80 | 100 | 120 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $h$ | 2 | 27 | 46 | 56 | 60 | 56 | 46 | 27 | 2 | -31 | -71 | -118 | -172 | -462 | -868 | -1390 |

