

Question	Scheme	Marks	AOs
<b>11(a)</b>	Midpoint = (8,0) or $m = \frac{-1-1}{11-5} \left\{ = -\frac{1}{3} \right\}$	B1	1.1b
	$y - "0" = "3"(x - "8")$	M1	1.1b
	$y = 3x - 24$	A1	1.1b
		(3)	
<b>(b)</b>	$3x - 24 = -\frac{1}{2}x + \frac{1}{2} \Rightarrow x = \{7\}$	M1	3.1a
	$y = 3 \times "7" - 24 = \{-3\}$	dM1	1.1b
	$(7, -3)^*$	A1*	2.1
		(3)	
<b>(c)</b>	e.g. $(5-7)^2 + (1+3)^2 = r^2$ leading to $r^2 = \{20\}$	M1	1.1b
	$(x-7)^2 + (y+3)^2 = 20$	A1	1.1b
		(2)	
<b>(d)</b>	<i>PR</i> : $y = 2x - 9$	B1	2.2a
	$(x-7)^2 + ("2x-9"+3)^2 = 20$	M1	3.1a
	$5x^2 - 38x + 65 = 0$ $(5x-13)(x-5) = 0$ $\Rightarrow x = \dots$	dM1	1.1b
	$x = \frac{13}{5}$	A1	2.2a
	$\left(\frac{13}{5}, -\frac{19}{5}\right)$	A1	1.1b
		(5)	

**(13 marks)**

**Notes:**

**(a)**

**B1:** Finds either the midpoint or a correct expression for the gradient of *PQ*

**B1:**  $y - y_1 = -\frac{1}{m_{PQ}}(x - x_1)$  with an attempt at the midpoint (must not be *P* or *Q*) and the negative

reciprocal of their  $m = -\frac{1}{3}$

If  $y = mx + c$  is used they must proceed as far as  $c = \dots$

**B1:**  $y = 3x - 24$  only

**(b)**

**M1:** Substitutes their answer to (a) into the given equation: " $3x - 24$ " =  $-\frac{1}{2}x + \frac{1}{2}$  and solves to find a value for  $x$

**dM1:** Attempts to find a value for  $y$  using this value for  $x$  in either equation.

**A1\*:**  $(7, -3)$  cso

**(c)**

**M1:** Attempts to find the radius of the circle or  $r^2$  by substituting either  $(5,1)$  or  $(11,-1)$  into  $(x-7)^2 + (y+3)^2 = r^2$  leading to  $r^2 = \dots$  or  $r = \dots \{ = \sqrt{20} \text{ or } 2\sqrt{5} \}$

**A1:**  $(x-7)^2 + (y+3)^2 = 20$  o.e.

**(d)**

**B1:** Correct equation for  $PR$  using  $y-1 = 2(x-5)$

If  $y = mx + c$  is used they must get to  $y = 2x - 9$  o.e.

**M1:** Substitutes their  $y = 2x - 9$  into their circle equation, i.e.,  $(x-7)^2 + (2x-9+3)^2 = 20$  and attempts to expand.

**dM1:** Attempts to form a 3TQ, set = 0 and solve for  $x$ .

**A1:** Deduces  $x = \frac{13}{5}$  (or rejects  $x = 5$ , which may be rejected later on as coordinates)

**A1:** Fully correct work leading to  $\left(\frac{13}{5}, -\frac{19}{5}\right)$  o.e. e.g.  $(2.6, -3.8)$  (and  $(5,1)$  rejected if seen)