

Question	Scheme	Marks	AOs
4	$\frac{(x+h)^2 - x^2}{h} = \frac{x^2 + 2xh + h^2 - x^2}{h}$	M1	2.1
	$= \frac{2xh + h^2}{h}$	A1	1.1b
	$\frac{dy}{dx} = \lim_{h \rightarrow 0} \frac{2xh + h^2}{h} = \lim_{h \rightarrow 0} (2x + h) = 2x^*$	A1*	2.5
		(3)	

(3 marks)

### Notes

**Note:** Throughout the question allow use of  $\delta x$  for  $h$  or any other letter e.g.  $\alpha$  if used consistently. If  $\delta x$  is used then you can condone e.g.  $\delta^2 x$  for  $\delta x^2$  as well as condoning e.g. poorly formed  $\delta$ 's

**M1:** Begins the process by writing down the gradient of the chord and attempts to expand the correct squared bracket – you can condone “poor” squaring e.g.  $(x+h)^2 = x^2 + h^2$  but the  $-x^2$  must be present.

**A1:** Reaches a correct fraction o.e. with the  $x^2$  terms cancelled out and with no algebraic errors, e.g.  $\frac{x^{\cancel{2}} + 2xh + h^2 - x^{\cancel{2}}}{h}$ ,  $2x+h$  is correct.

**A1\*:** Completes the process by applying a limiting argument and deduces that  $\frac{dy}{dx} = 2x$  with no errors seen. They must have  $= 2x$  and not just  $\lim_{h \rightarrow 0} 2x$  to complete the proof.

$\frac{dy}{dx} =$  or an equivalent e.g.  $f'(x) =$  or “Gradient =” must be evident somewhere in their working or final line. If  $f'(x)$  is used then there is no requirement to see  $f(x)$  defined first. Condone e.g.  $\frac{dy}{dx} \rightarrow 2x$  or  $f'(x) \rightarrow 2x$ .

Condone missing brackets to allow e.g.  $\frac{dy}{dx} = \lim_{h \rightarrow 0} \frac{2xh + h^2}{h} = \lim_{h \rightarrow 0} 2x + h = 2x$

Do not allow  $h = 0$  if there is never a reference to  $h \rightarrow 0$ .

e.g.  $\frac{dy}{dx} = \lim_{h \rightarrow 0} \frac{2xh + h^2}{h} = \lim_{h \rightarrow 0} 2x + 0 = 2x$  is acceptable

but e.g.  $\frac{dy}{dx} = \frac{2xh + h^2}{h} = 2x + 0 = 2x$  is not unless  $h \rightarrow 0$  is seen.

The  $h \rightarrow 0$  does not need to be present throughout the proof e.g. appear on every line but must appear at least once.

They must reach  $2x+h$  at the end and not  $\frac{2xh + h^2}{h}$  (without the  $h$ 's cancelled) to complete the limiting argument.