

8. The functions  $f$  and  $g$  are defined by

$$f(x) = 4 - 3x^2 \quad x \in \mathbb{R}$$

$$g(x) = \frac{5}{2x - 9} \quad x \in \mathbb{R}, x \neq \frac{9}{2}$$

(a) Find  $fg(2)$

**(2)**

(b) Find  $g^{-1}$

**(3)**

(c) (i) Find  $gf(x)$ , giving your answer as a simplified fraction.

(ii) Deduce the range of  $gf(x)$ .

**(3)**

The function  $h$  is defined by

$$h(x) = 2x^2 - 6x + k \quad x \in \mathbb{R}$$

where  $k$  is a constant.

(d) Find the range of values of  $k$  for which the equation

$$f(x) = h(x)$$

has no real solutions.

**(3)**