

Question	Scheme	Marks	AOs
11(a)	$(R =) \sqrt{185}$	B1	1.1b
	$\tan \alpha = \frac{13}{4} \Rightarrow \alpha = \dots$	M1	1.1b
	$\alpha = \text{awrt } 1.272 \text{ or } \sqrt{185} \cos(x + 1.272)$	A1	1.1b
		(3)	
(b)(i)	$30 - \sqrt{185} \text{ or awrt } 16.4$	B1ft	2.2a
(b)(ii)	$\cos\left(\frac{\pi t}{12} + 1.272 + 0.2\right) = -1 \Rightarrow \frac{\pi t}{12} + 1.272 + 0.2 = \pi \Rightarrow t = ..$	M1	3.1b
	$(t =) \text{awrt } 6.4$	A1	1.1b
	6:22 or 6:23 oe (see notes)	B1ft	3.2a
		(4)	
(c)	$D = 30 + \sqrt{185} \cos\left(\frac{\pi t}{12} + 1.272 + 0.2\right)$ $\Rightarrow \left(\frac{dD}{dt} =\right) - \frac{\pi \sqrt{185}}{12} \sin\left(\frac{\pi t}{12} + 1.272 + 0.2\right)$	M1	3.4
	$3\text{pm} \rightarrow t = 15$ $\Rightarrow \left(\frac{dD}{dt} =\right) - \frac{\pi \sqrt{185}}{12} \sin\left(\frac{15\pi}{12} + 1.272 + 0.2\right)$	dM1	3.1b
	$\Rightarrow (k =) \text{awrt } 2.75$	A1	1.1b
		(3)	
(d)	Examples: - the demand for electricity is not the same every day - during cold weather the demand will be greater - in the summer, demand will be less	B1	3.5b
		(1)	

(11 marks)

Notes

(a) Note that B0M1A1 is possible

B1: $\sqrt{185}$

M1: Award for $\tan \alpha = \pm \frac{13}{4} \Rightarrow \alpha = \dots$, $\tan \alpha = \pm \frac{4}{13} \Rightarrow \alpha = \dots$,

$\sin \alpha = \pm \frac{13}{\sqrt{185}} \Rightarrow \alpha = \dots$ or $\cos \alpha = \pm \frac{4}{\sqrt{185}} \Rightarrow \alpha = \dots$

May be implied by ($\pm$) any of awrt 1.27 or awrt 72.9° or awrt 0.298 or awrt 17.1° or awrt 1.87 or awrt 107°

A1: $\alpha = \text{awrt } 1.272 \text{ or } \sqrt{185} \cos(x + 1.272)$

Note that $\sqrt{185} \cos(x + 1.272)$ scores B1M1A1

Mark (b)(i) and(ii) together

(b)(i)

B1ft: $(30 - \sqrt{185})$ (GW) **or** awrt 16.4 (GW) Condone lack of / ignore units and follow through on their R to 3sf

(ii)

M1: Sets $\frac{\pi t}{12} + "1.272" + 0.2 = \pi \Rightarrow t = ..$ May be implied by a correct value for t for their "1.272". If just a value is stated you may need to check this on your calculator.

May set $"30 + \sqrt{185} \cos\left(\frac{\pi t}{12} + 1.272 + 0.2\right)" = \underline{30 - \sqrt{185}} \Rightarrow t = ...$ but condone if they have rounded $\underline{30 - \sqrt{185}}$ to 3sf or better.

A1: awrt 6.4 and no others in the range $0 < t < 24$ unless rejected. This can be implied by 6:22 or 6:23 oe and no additional times given.

If no value for t is given then allow to be implied by 6:22 or 6:23 oe

B1ft 6:22 or 6:23 oe or ft on their final t to nearest min or truncated **provided** $0 < "t" < 24$ e.g. 0622 or 6 hours 23 minutes after midnight. Condone various notation or forms provided there is evidence of the correct time. E.g. 6:23am 6.22 or 6,23 or 6;23 or 6/22. If using e.g. am or pm it must be consistent with their value of t .

(c) Note that no differentiation seen scores M0dM0A0.

M1: Attempts to differentiate their $D = 30 + \sqrt{185} \cos\left(\frac{\pi t}{12} + q\right)$ to obtain $... \sin\left(\frac{\pi t}{12} + q\right)$ where $q = "1.272" + 0.2$ oe or condone if 0.2 is missing

Condone also differentiating $D = 30 + 4 \cos\left(\frac{\pi t}{12} + 0.2\right) - 13 \sin\left(\frac{\pi t}{12} + 0.2\right)$ to obtain $... \sin\left(\frac{\pi t}{12} + 0.2\right) + ... \cos\left(\frac{\pi t}{12} + 0.2\right)$

NB correct derivative is $-\frac{4\pi}{12} \sin\left(\frac{\pi t}{12} + 0.2\right) - \frac{13\pi}{12} \cos\left(\frac{\pi t}{12} + 0.2\right)$

dM1: Substitutes $t = 15$ into their derivative and obtains a value. It is dependent on the previous method mark. 15 embedded in their derivative followed by a value or stating when $t = 15$, $\frac{dD}{dt} = ...$ is sufficient but if just a value is stated with no working

then you may need to check this value is correct for their $\frac{dD}{dt}$ (condone mislabelling)

A1: awrt 2.75

(d)

B1: for a valid reason why it would not be sensible to use the same equation to model the demand for electricity in the UK on **every day of the year**. Mark positively.

Look for any reason that suggests the demand is not the same **every day** or it is **different to this particular day**. They either need to:

- suggest the demand is not the same every day such as
 - it varies at different times of the year / the length of day(light) varies
 - this was only for a particular day
- suggest a possible scenario where the demand might be different such as
 - it is different at weekends
 - may have dinner at a different time of day on a Sunday
 - might introduce an incentive scheme
 - the price cap might affect how much people use
 - people might go abroad in school holidays

Do not allow “we do not have enough data” (too vague)