

Question	Scheme	Marks	AOs
<b>14(a)</b>	Sets $500 = \pi r^2 h$	B1	2.1
	Substitute $h = \frac{500}{\pi r^2}$ into $S = 2\pi r^2 + 2\pi r h = 2\pi r^2 + 2\pi r \times \frac{500}{\pi r^2}$	M1	2.1
	Simplifies to reach given answer $S = 2\pi r^2 + \frac{1000}{r}$ *	A1*	1.1b
		<b>(3)</b>	
<b>(b)</b>	Differentiates $S$ with both indices correct in $\frac{dS}{dr}$	M1	3.4
	$\frac{dS}{dr} = 4\pi r - \frac{1000}{r^2}$	A1	1.1b
	Sets $\frac{dS}{dr} = 0$ and proceeds to $r^3 = k$ , $k$ is a constant	M1	2.1
	Radius = 4.30 cm	A1	1.1b
	Substitutes their $r = 4.30$ into $h = \frac{500}{\pi r^2} \Rightarrow$ Height = 8.60 cm	A1	1.1b
		<b>(5)</b>	
<b>(c)</b>	States a valid reason such as <ul style="list-style-type: none"> <li>The radius is too big for the size of our hands</li> <li>If <math>r = 4.3</math> cm and <math>h = 8.6</math> cm the can is square in profile. All drinks cans are taller than they are wide</li> <li>The radius is too big for us to drink from</li> <li>They have different dimensions to other drinks cans and would be difficult to stack on shelves with other drinks cans</li> </ul>	B1	3.2a
		<b>(1)</b>	

**9 marks**

**Notes:**

**(a)**

**B1:** Uses the correct volume formula with  $V=500$ . Accept  $500 = \pi r^2 h$

**M1:** Substitutes  $h = \frac{500}{\pi r^2}$  or  $rh = \frac{500}{\pi r}$  into  $S = 2\pi r^2 + 2\pi r h$  to get  $S$  as a function of  $r$

**A1\*:**  $S = 2\pi r^2 + \frac{1000}{r}$  Note that this is a given answer.

**(b)**

**M1:** Differentiates the given  $S$  to reach  $\frac{dS}{dr} = Ar \pm Br^{-2}$

**A1:**  $\frac{dS}{dr} = 4\pi r - \frac{1000}{r^2}$  or exact equivalent

**M1:** Sets  $\frac{dS}{dr} = 0$  and proceeds to  $r^3 = k$ ,  $k$  is a constant

**A1:**  $R =$  awrt 4.30cm

**A1:**  $H =$  awrt 8.60 cm

**(c)**

**B1:** Any valid reason. See scheme for alternatives