

Question	Scheme	Marks	AOs
<b>15</b>	$\frac{dy}{dx} = \frac{15}{2}x^{\frac{1}{2}} - 9$	M1 A1	3.1a 1.1b
	Substitutes $x = 4 \Rightarrow \frac{dy}{dx} = 6$	M1	2.1
	Uses (4, 15) and gradient $\Rightarrow y - 15 = 6(x - 4)$	M1	2.1
	Equation of $l$ is $y = 6x - 9$	A1	1.1b
	Area $R = \int_0^4 \left( 5x^{\frac{3}{2}} - 9x + 11 \right) - (6x - 9) dx$	M1	3.1a
	$= \left[ 2x^{\frac{5}{2}} - \frac{15}{2}x^2 + 20x(+c) \right]_0^4$	A1	1.1b
	Uses both limits of 4 and 0 $\left[ 2x^{\frac{5}{2}} - \frac{15}{2}x^2 + 20x \right]_0^4 = 2 \times 4^{\frac{5}{2}} - \frac{15}{2} \times 4^2 + 20 \times 4 - 0$	M1	2.1
	Area of $R = 24$ *	A1*	1.1b
	Correct notation with good explanations	A1	2.5
	<b>(10)</b>		
<b>(10 marks)</b>			

Notes:

**M1:** Differentiates  $5x^{\frac{3}{2}} - 9x + 11$  to a form  $Ax^{\frac{1}{2}} + B$

**A1:**  $\frac{dy}{dx} = \frac{15}{2}x^{\frac{1}{2}} - 9$  but may not be simplified

**M1:** Substitutes  $x = 4$  in their  $\frac{dy}{dx}$  to find the gradient of the tangent

**M1:** Uses their gradient and the point (4, 15) to find the equation of the tangent

**A1:** Equation of  $l$  is  $y = 6x - 9$

**M1:** Uses Area  $R = \int_0^4 \left( 5x^{\frac{3}{2}} - 9x + 11 \right) - (6x - 9) dx$  following through on their  $y = 6x - 9$

Look for a form  $Ax^{\frac{5}{2}} + Bx^2 + Cx$

**A1:**  $= \left[ 2x^{\frac{5}{2}} - \frac{15}{2}x^2 + 20x(+c) \right]_0^4$  This must be correct but may not be simplified

**M1:** Substitutes in both limits and subtracts

**A1\*:** Correct area for  $R = 24$

**A1:** Uses correct notation and produces a well explained and accurate solution. Look for

- Correct notation used consistently and accurately for both differentiation and integration
- Correct explanations in producing the equation of  $l$ . See scheme.
- Correct explanation in finding the area of  $R$ . In way 2 a diagram may be used.

Alternative method for the area using area under curve and triangles. (Way 2)

**M1:** Area under curve  $= \int_0^4 \left( 5x^{\frac{3}{2}} - 9x + 11 \right) = \left[ Ax^{\frac{5}{2}} + Bx^2 + Cx \right]_0^4$

**A1:**  $= \left[ 2x^{\frac{5}{2}} - \frac{9}{2}x^2 + 11x \right]_0^4 = 36$

**M1:** This requires a full method with all triangles found using a correct method

Look for Area  $R =$  their  $36 - \frac{1}{2} \times 15 \times \left( 4 - \text{their } \frac{3}{2} \right) + \frac{1}{2} \times \text{their } 9 \times \text{their } \frac{3}{2}$