

Question	Scheme	Marks	AOs
6(a)	$f(x) = (8 - x)\ln x, x > 0$		
	Crosses x -axis $\Rightarrow f(x) = 0 \Rightarrow (8 - x)\ln x = 0$		
	x coordinates are 1 and 8	B1	1.1b
		(1)	
(b)	Complete strategy of setting $f'(x) = 0$ and rearranges to make $x = \dots$	M1	3.1a
	$\left\{ \begin{array}{l} u = (8 - x) \quad v = \ln x \\ \frac{du}{dx} = -1 \quad \frac{dv}{dx} = \frac{1}{x} \end{array} \right\}$		
	$f'(x) = -\ln x + \frac{8-x}{x}$	M1	1.1b
		A1	1.1b
	$-\ln x + \frac{8-x}{x} = 0 \Rightarrow -\ln x + \frac{8}{x} - 1 = 0$ $\Rightarrow \frac{8}{x} = 1 + \ln x \Rightarrow x = \frac{8}{1 + \ln x} \quad *$	A1*	2.1
	(4)		
(c)	Evaluates both $f'(3.5)$ and $f'(3.6)$	M1	1.1b
	$f'(3.5) = 0.032951317\dots$ and $f'(3.6) = -0.058711623\dots$ Sign change and as $f'(x)$ is continuous, the x coordinate of Q lies between $x = 3.5$ and $x = 3.6$	A1	2.4
		(2)	
(d)(i)	$\{x_5 =\} 3.5340$	B1	1.1b
(d)(ii)	$\{x_Q =\} 3.54$ (2 dp)	B1	2.2a
		(2)	
(9 marks)			

Question 6 Notes:

(a)

B1: Either

- 1 and 8
- on Figure 2, marks 1 next to A and 8 next to B

(b)

M1: Recognises that Q is a stationary point (and not a root) and applies a complete strategy of setting $f'(x) = 0$ and rearranges to make $x = \dots$

M1: Applies $vu' + uv'$, where $u = 8 - x$, $v = \ln x$

Note: This mark can be recovered for work in part (c)

A1: $(8 - x)\ln x \rightarrow -\ln x + \frac{8 - x}{x}$, or equivalent

Note: This mark can be recovered for work in part (c)

A1*: Correct proof with no errors seen in working.

(c)

M1: Evaluates both $f'(3.5)$ and $f'(3.6)$

A1: $f'(3.5) = \text{awrt } 0.03$ and $f'(3.6) = \text{awrt } -0.06$ or $f'(3.6) = -0.05$ (truncated)

and a correct conclusion

(d)(i)

B1: See scheme

(d)(ii)

B1: Deduces (e.g. by the use of further iterations) that the x coordinate of Q is 3.54 accurate to 2 dp

Note: $3.5 \rightarrow 3.55119 \rightarrow 3.52845 \rightarrow 3.53848 \rightarrow 3.53404 \rightarrow 3.53600 \rightarrow 3.53514 (\rightarrow 3.535518\dots)$