

Question	Scheme	Marks	AOs
12	Complete process to find at least one set of coordinates for P . The process must include evidence of <ul style="list-style-type: none"> differentiating setting $\frac{dy}{dx} = 0$ to find $x = \dots$ substituting $x = \dots$ into $\sin x + \cos y = 0.5$ to find $y = \dots$ 	M1	3.1a
	$\left\{ \begin{array}{l} \frac{dy}{dx} \\ \frac{dy}{dx} \end{array} \right\} \times \cos x - \sin y \frac{dy}{dx} = 0$	B1	1.1b
	Applies $\frac{dy}{dx} = 0$ (e.g. $\cos x = 0$ or $\frac{\cos x}{\sin y} = 0 \Rightarrow \cos x = 0 \Rightarrow x = \dots$)	M1	2.2a
	giving at least one of either $x = -\frac{\pi}{2}$ or $x = \frac{\pi}{2}$	A1	1.1b
	$x = \frac{\pi}{2} \Rightarrow \sin\left(\frac{\pi}{2}\right) + \cos y = 0.5 \Rightarrow \cos y = -\frac{1}{2} \Rightarrow y = \frac{2\pi}{3}$ or $-\frac{2\pi}{3}$	M1	1.1b
	So in specified range, $(x, y) = \left(\frac{\pi}{2}, \frac{2\pi}{3}\right)$ and $\left(\frac{\pi}{2}, -\frac{2\pi}{3}\right)$, by cso	A1	1.1b
	$x = -\frac{\pi}{2} \Rightarrow \sin\left(-\frac{\pi}{2}\right) + \cos y = 0.5 \Rightarrow \cos y = 1.5$ has no solutions, and so there are exactly 2 possible points P .	B1	2.1
	(7)		

(7 marks)

Question 12 Notes:

M1: See scheme

B1: Correct differentiated equation. E.g. $\cos x - \sin y \frac{dy}{dx} = 0$

M1: Uses the information “the tangent to C at the point P is parallel to the x -axis” to deduce and apply $\frac{dy}{dx} = 0$ and finds $x = \dots$

A1: See scheme

M1: For substituting one of their values from $\frac{dy}{dx} = 0$ into $\sin x + \cos y = 0.5$ and so finds $x = \dots, y = \dots$

A1: Selects coordinates for P on C satisfying $\frac{dy}{dx} = 0$ and $-\frac{\pi}{2} \leq x < \frac{3\pi}{2}, -\pi < y < \pi$
i.e. finds $\left(\frac{\pi}{2}, \frac{2\pi}{3}\right)$ and $\left(\frac{\pi}{2}, -\frac{2\pi}{3}\right)$ and no other points by correct solution only

B1: Complete argument to show that there are exactly 2 possible points P .