

Question	Scheme	Marks	AOs
<b>13(a)</b>	$\operatorname{cosec}2x + \cot 2x \equiv \cot x, \quad x \neq 90n^\circ, \quad n \in \mathbb{Z}$		
	$\operatorname{cosec}2x + \cot 2x = \frac{1}{\sin 2x} + \frac{\cos 2x}{\sin 2x}$	M1	1.2
	$= \frac{1 + \cos 2x}{\sin 2x}$	M1	1.1b
	$= \frac{1 + 2\cos^2 x - 1}{2\sin x \cos x} = \frac{2\cos^2 x}{2\sin x \cos x}$	M1	2.1
		A1	1.1b
	$= \frac{\cos x}{\sin x} = \cot x \quad *$	A1*	2.1
	<b>(5)</b>		
<b>(b)</b>	$\operatorname{cosec}(4\theta + 10^\circ) + \cot(4\theta + 10^\circ) = \sqrt{3}; \quad 0^\circ < \theta < 180^\circ,$		
	$\cot(2\theta \pm \dots^\circ) = \sqrt{3}$	M1	2.2a
	$2\theta \pm \dots = 30^\circ \Rightarrow \theta = 12.5^\circ$	M1	1.1b
		A1	1.1b
	$2\theta + 5^\circ = 180^\circ + PV^\circ \Rightarrow \theta = \dots^\circ$	M1	2.1
	$\theta = 102.5^\circ$	A1	1.1b
	<b>(5)</b>		
<b>(10 marks)</b>			

Question 13 Notes:

**(a)**

**M1:** Writes  $\operatorname{cosec}2x = \frac{1}{\sin 2x}$  and  $\cot 2x = \frac{\cos 2x}{\sin 2x}$

**M1:** Combines into a single fraction with a common denominator

**M1:** Applies  $\sin 2x = 2\sin x \cos x$  to the denominator **and** applies either

- $\cos 2x = 2\cos^2 x - 1$
- $\cos 2x = 1 - 2\sin^2 x$  and  $\sin^2 x + \cos^2 x = 1$
- $\cos 2x = \cos^2 x - \sin^2 x$  and  $\sin^2 x + \cos^2 x = 1$

to the numerator and manipulates to give a one term numerator expression

**A1:** Correct algebra leading to  $\frac{2\cos^2 x}{2\sin x \cos x}$  or equivalent.

**A1\*:** Correct proof with correct notation and no errors seen in working

**(b)**

**M1:** Uses the result in part (a) in an attempt to deduce either  $2x = 4\theta + 10$  or  $x = 2\theta + \dots$  and uses  $x = 2\theta + \dots$  to write down or imply  $\cot(2q \pm \dots^\circ) = \sqrt{3}$

**M1:** Applies  $\operatorname{arccot}(\sqrt{3}) = 30^\circ$  or  $\operatorname{arctan}\left(\frac{1}{\sqrt{3}}\right) = 30^\circ$

and attempts to solve  $2\theta \pm \dots = 30^\circ$  to give  $\theta = \dots$

**A1:** Uses a correct method to obtain  $\theta = 12.5^\circ$

**M1:** Uses  $2\theta + 5 = 180 + \text{their } PV^\circ$  in a complete method to find the second solution,  $\theta = \dots$

**A1:** Uses a correct method to obtain  $\theta = 102.5^\circ$ , with no extra solutions given either inside or outside the required range  $0, \theta < 180^\circ$