2. (a) Given that  $\theta$  is small, use the small angle approximation for  $\cos \theta$  to show that

$$1 + 4\cos\theta + 3\cos^2\theta \approx 8 - 5\theta^2$$

Adele uses  $\theta = 5^{\circ}$  to test the approximation in part (a).

Adele's working is shown below.

Using my calculator,  $1 + 4\cos(5^\circ) + 3\cos^2(5^\circ) = 7.962$ , to 3 decimal places. Using the approximation  $8 - 5\theta^2$  gives  $8 - 5(5)^2 = -117$ Therefore,  $1 + 4\cos\theta + 3\cos^2\theta \approx 8 - 5\theta^2$  is not true for  $\theta = 5^\circ$ 

- (b) (i) Identify the mistake made by Adele in her working.
  - (ii) Show that  $8 5\theta^2$  can be used to give a good approximation to  $1 + 4\cos\theta + 3\cos^2\theta$  for an angle of size  $5^{\circ}$

(3)