

Question	Scheme	Marks	AOs
1	$g(x) = \frac{2x+5}{x-3}, x \geq 5$		
(a) Way 1	$g(5) = \frac{2(5)+5}{5-3} = 7.5 \Rightarrow gg(5) = \frac{2("7.5")+5}{"7.5"-3}$	M1	1.1b
	$gg(5) = \frac{40}{9} \left( \text{or } 4\frac{4}{9} \text{ or } 4.\dot{4} \right)$	A1	1.1b
		(2)	
(a) Way 2	$gg(x) = \frac{2\left(\frac{2x+5}{x-3}\right)+5}{\left(\frac{2x+5}{x-3}\right)-3} \Rightarrow gg(5) = \frac{2\left(\frac{2(5)+5}{(5)-3}\right)+5}{\left(\frac{2(5)+5}{(5)-3}\right)-3}$	M1	1.1b
	$gg(5) = \frac{40}{9} \left( \text{or } 4\frac{4}{9} \text{ or } 4.\dot{4} \right)$	A1	1.1b
		(2)	
(b)	{Range:} $2 < y \leq \frac{15}{2}$	B1	1.1b
		(1)	
(c) Way 1	$y = \frac{2x+5}{x-3} \Rightarrow yx - 3y = 2x+5 \Rightarrow yx - 2x = 3y+5$	M1	1.1b
	$x(y-2) = 3y+5 \Rightarrow x = \frac{3y+5}{y-2} \left\{ \text{or } y = \frac{3x+5}{x-2} \right\}$	M1	2.1
	$g^{-1}(x) = \frac{3x+5}{x-2}, 2 < x \leq \frac{15}{2}$	A1ft	2.5
		(3)	
(c) Way 2	$y = \frac{2x-6+11}{x-3} \Rightarrow y = 2 + \frac{11}{x-3} \Rightarrow y-2 = \frac{11}{x-3}$	M1	1.1b
	$x-3 = \frac{11}{y-2} \Rightarrow x = \frac{11}{y-2} + 3 \left\{ \text{or } y = \frac{11}{x-2} + 3 \right\}$	M1	2.1
	$g^{-1}(x) = \frac{11}{x-2} + 3, 2 < x \leq \frac{15}{2}$	A1ft	2.5
		(3)	

(6 marks)

### Notes for Question 1

(a)	
M1:	Full method of attempting $g(5)$ and substituting the result into $g$
Note:	Way 2: Attempts to substitute $x=5$ into $\frac{2\left(\frac{2x+5}{x-3}\right)+5}{\left(\frac{2x+5}{x-3}\right)-3}$ , o.e. Note that $gg(x) = \frac{9x-5}{14-x}$
A1:	Obtains $\frac{40}{9}$ or $4\frac{4}{9}$ or $4.\dot{4}$ or an exact equivalent
Note:	Give A0 for $4.4$ or $4.444\dots$ without reference to $\frac{40}{9}$ or $4\frac{4}{9}$ or $4.\dot{4}$

### Notes for Question 1 Continued

<b>(b)</b>	
<b>B1:</b>	States $2 < y \leq \frac{15}{2}$ Accept any of $2 < g \leq \frac{15}{2}$ , $2 < g(x) \leq \frac{15}{2}$ , $\left(2, \frac{15}{2}\right]$
<b>Note:</b>	Accept $g(x) > 2$ <b>and</b> $g(x) \leq \frac{15}{2}$ o.e.
<b>(c)</b>	
<b>Way 1</b>	
<b>M1:</b>	Correct method of cross multiplication followed by an attempt to collect terms in $x$ or terms in a swapped $y$
<b>M1:</b>	A complete method (i.e. as above and also factorising and dividing) to find the inverse
<b>A1ft:</b>	Uses correct notation to correctly define the inverse function $g^{-1}$ , where the domain of $g^{-1}$ stated correctly or correctly followed through (using correct notation) on the values shown in their range in part (b). Allow $g^{-1}: x \rightarrow$ . Condone $g^{-1} = \dots$ Do not accept $y = \dots$
<b>Note:</b>	Correct notation is required when stating the domain of $g^{-1}(x)$ . Allow $2 < x \leq \frac{15}{2}$ or $\left(2, \frac{15}{2}\right]$  Do not allow any of e.g. $2 < g \leq \frac{15}{2}$ , $2 < g^{-1}(x) \leq \frac{15}{2}$
<b>Note:</b>	Do not allow A1ft for following through their range in (b) to give a domain for $g^{-1}$ as $x \in \mathbb{R}$
<b>(c)</b>	
<b>Way 2</b>	
<b>M1:</b>	Writes $y = \frac{2x+5}{x-3}$ in the form $y = 2 \pm \frac{k}{x-3}$ , $k \neq 0$ and rearranges to isolate $y$ and 2 on one side of their equation. <b>Note:</b> Allow the equivalent method with $x$ swapped with $y$
<b>M1:</b>	A complete method to find the inverse
<b>A1ft:</b>	As in Way 1
<b>Note:</b>	If a candidate scores no marks in part (c), but <ul style="list-style-type: none"> <li>• states the domain of <math>g^{-1}</math> correctly, <b>or</b></li> <li>• states a domain of <math>g^{-1}</math> which is correctly followed through on the values shown in their range in part (b)</li> </ul> then give special case (SC) M1 M0 A0