

Question	Scheme	Marks	AOs
1	$\cos \theta - \sin\left(\frac{1}{2}\theta\right) + 2 \tan \theta = \frac{11}{10}$		
(a)	$1 - \frac{1}{2}\theta^2 - \frac{1}{2}\theta + 2\theta \approx \frac{11}{10}$	M1	1.2
	$\Rightarrow \frac{1}{2}\theta^2 - \frac{3}{2}\theta + \frac{1}{10} \approx 0 \Rightarrow 5\theta^2 - 15\theta + 1 \approx 0 *$	A1	1.1b
		A1*	2.1
		(3)	
(b)	$\theta = 0.068$ is valid because θ is small $\theta = 2.932$ is not valid because θ is large	B1	2.3
		(1)	

(4 marks)

Question 1 Notes:

- (a)**
- M1:** At least two of either $\cos \theta \approx 1 - \frac{1}{2}\theta^2$, $\sin\left(\frac{1}{2}\theta\right) \approx \frac{1}{2}\theta$ or $\tan \theta \approx \theta$ substituted into the given equation
- A1:** Substitutes $\cos \theta \approx 1 - \frac{1}{2}\theta^2$, $\sin\left(\frac{1}{2}\theta\right) \approx \frac{1}{2}\theta$ and $\tan \theta \approx \theta$ into the given equation to obtain a correct (un-simplified) approximation or equation. E.g. $1 - \frac{1}{2}\theta^2 - \frac{1}{2}\theta + 2\theta \approx \frac{11}{10}$ or $= \frac{11}{10}$
- A1*:** Obtains $5\theta^2 - 15\theta + 1 \approx 0$ (condone $5\theta^2 - 15\theta + 1 = 0$) with no errors seen in their working
- (b)**
- B1:** States $\theta = 0.068$ is valid because θ is small; and $\theta = 2.932$ is not valid because θ is large

- (b)**
- Alt 1** LHS = $\cos \theta - \sin\left(\frac{1}{2}\theta\right) + 2 \tan \theta$
- B1:** States $\theta = 0.068$ is valid and $\theta = 2.932$ is not valid based on testing these two values in the original equation
- Note:** $\theta = 0.068 \Rightarrow \text{LHS} = 1.0999\dots$ & $\theta = 2.932 \Rightarrow \text{LHS} = -2.3980\dots$

Note: $\theta = 0.068218\dots \Rightarrow \text{LHS} = 1.1002\dots$ & $\theta = 2.931782\dots \Rightarrow \text{LHS} = -2.3984\dots$