| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 4 | $C_{1}: x=10 \cos t, y=4 \sqrt{2} \sin t, 0 \leq t<2 \pi ; \quad C_{2}: x^{2}+y^{2}=66$ |  |  |
| Way 1 | $(10 \cos t)^{2}+(4 \sqrt{2} \sin t)^{2}=66$ | M1 | 3.1a |
|  | $100\left(1-\sin ^{2} t\right)+32 \sin ^{2} t=66$ | M1 | 2.1 |
|  |  | A1 | 1.1 b |
|  | $\begin{array}{c\|c} \hline 100-68 \sin ^{2} t=66 \Rightarrow \sin ^{2} t=\frac{1}{2} & 68 \cos ^{2} t+32=66 \Rightarrow \cos ^{2} t=\frac{1}{2} \\ \Rightarrow \sin t=\ldots & \Rightarrow \cos t=\ldots \end{array}$ | dM1 | 1.1b |
|  | Substitutes their solution back into the relevant original equation(s) <br> to get the value of the $x$-coordinate and value of the corresponding $y$-coordinate. <br> Note: These may not be in the correct quadrant | M1 | 1.1b |
|  | $S=(5 \sqrt{2},-4)$ or $x=5 \sqrt{2}, y=-4$ or $S=($ awrt $7.07,-4)$ | A1 | 3.2 a |
|  |  | (6) |  |
| Way 2 | $\left\{\cos ^{2} t+\sin ^{2} t=1 \Rightarrow\right\}\left(\frac{x}{10}\right)^{2}+\left(\frac{y}{4 \sqrt{2}}\right)^{2}=1\left\{\Rightarrow 32 x^{2}+100 y^{2}=3200\right\}$ | M1 | 3.1a |
|  | $\frac{x^{2}}{10}+\frac{66-x^{2}}{32}=1 \quad \frac{66-y^{2}}{100}+\frac{y^{2}}{32}=1$ | M1 | 2.1 |
|  | $\overline{100}+\frac{32}{32}=100{ }^{\text {a }}+\frac{y^{32}}{32}=1$ | A1 | 1.1 b |
|  | $32 x^{2}+6600-100 x^{2}=3200$ $2112-32 y^{2}+100 y^{2}=3200$ <br> $x^{2}=50 \Rightarrow x=\ldots$ $y^{2}=16 \Rightarrow y=\ldots$ | dM1 | 1.1b |
|  | Substitutes their solution back into the relevant original equation(s) to get the value of the corresponding $x$-coordinate or $y$-coordinate. <br> Note: These may not be in the correct quadrant | M1 | 1.1b |
|  | $S=(5 \sqrt{2},-4)$ or $x=5 \sqrt{2}, y=-4$ or $S=($ awrt $7.07,-4)$ | A1 | 3.2a |
|  |  | (6) |  |
| Way 3 | $\begin{gathered} \left\{C_{2}: x^{2}+y^{2}=66 \Rightarrow\right\} \quad x=\sqrt{66} \cos \alpha, y=\sqrt{66} \sin \alpha \\ \left\{C_{1}=C_{2} \Rightarrow\right\} \quad 10 \cos t=\sqrt{66} \cos \alpha, \quad 4 \sqrt{2} \sin t=\sqrt{66} \sin \alpha \\ \left\{\cos ^{2} \alpha+\sin ^{2} \alpha=1 \Rightarrow\right\}\left(\frac{10 \cos t}{\sqrt{66}}\right)^{2}+\left(\frac{4 \sqrt{2} \sin t}{\sqrt{66}}\right)^{2}=1 \end{gathered}$ | M1 | 3.1a |
|  | then continue with applying the mark scheme for Way 1 |  |  |
| Way 4 | $(10 \cos t)^{2}+(4 \sqrt{2} \sin t)^{2}=66$ | M1 | 3.1a |
|  | $100\left(\frac{1+\cos 2 t}{2}\right)+32\left(\frac{1-\cos 2 t}{2}\right)=66$ | M1 | 2.1 |
|  | $100\left(\frac{1}{2}\right)+32\left(\frac{\cos 2 t}{2}\right)=66$ | A1 | 1.1 b |
|  | $\begin{gathered} 50+50 \cos 2 t+16-16 \cos 2 t=66 \Rightarrow 34 \cos 2 t+66=66 \\ \Rightarrow \cos 2 t=\ldots \end{gathered}$ | dM1 | 1.1b |
|  | Substitutes their solution back into the original equation(s) to get the value of the $x$-coordinate and value of the $y$-coordinate. <br> Note: These may not be in the correct quadrant | M1 | 1.1b |
|  | $S=(5 \sqrt{2},-4)$ or $x=5 \sqrt{2}, y=-4$ or $S=($ awrt $7.07,-4)$ | A1 | 3.2a |
|  |  | (6) |  |
|  | Note: Give final A0 for writing $x=5 \sqrt{2}, y=-4$ followed by $S=(-4,5 \sqrt{2})$ |  |  |
| (6 marks) |  |  |  |
| Notes for Question 4 |  |  |  |


|  | Way 1 |
| :---: | :---: |
| M1: | Begins to solve the problem by applying an appropriate strategy. <br> E.g. Way 1: A complete process of combining equations for $C_{1}$ and $C_{2}$ by substituting the parametric equation into the Cartesian equation to give an equation in one variable (i.e. $t$ ) only. |
| M1: | Uses the identity $\sin ^{2} t+\cos ^{2} t \equiv 1$ to achieve an equation in $\sin ^{2} t$ only or $\cos ^{2} t$ only |
| A1: | A correct equation in $\sin ^{2} t$ only or $\cos ^{2} t$ only |
| dM1: Note: | dependent on both the previous $M$ marks <br> Rearranges to make $\sin t=\ldots$ where $-1 \leq \sin t \leq 1$ or $\cos t=\ldots$ where $-1 \leq \cos t \leq 1$ <br> Condone $3{ }^{\text {rd }} \mathrm{M} 1$ for $\sin ^{2} t=\frac{1}{2} \Rightarrow \sin t=\frac{1}{4}$ |
| M1: | See scheme |
| A1: | Selects the correct coordinates for $S$ Allow either $S=(5 \sqrt{2},-4)$ or $S=($ awrt $7.07,-4)$ |
|  | Way 2 |
| M1: | Begins to solve the problem by applying an appropriate strategy. <br> E.g. Way 2: A complete process of using $\cos ^{2} t+\sin ^{2} t \equiv 1$ to convert the parametric equation for $C_{1}$ into a Cartesian equation for $C_{1}$ |
| M1: | Complete valid attempt to write an equation in terms of $x$ only or $y$ only not involving trigonometry |
| A1: | A correct equation in $x$ only or $y$ only not involving trigonometry |
| dM1: Note: | dependent on both the previous $M$ marks Rearranges to make $x=\ldots$ or $y=\ldots$ their $x^{2}$ or their $y^{2}$ must be $>0$ for this mark |
| M1: <br> Note: | See scheme their $x^{2}$ and their $y^{2}$ must be $>0$ for this mark |
| A1: | Selects the correct coordinates for $S$ <br> Allow either $S=(5 \sqrt{2},-4)$ or $S=($ awrt $7.07,-4)$ or $S=(\sqrt{50},-4)$ or $S=\left(\frac{10}{\sqrt{2}},-4\right)$ |
|  | Way 3 |
| M1: | Begins to solve the problem by applying an appropriate strategy. <br> E.g. Way 3: A complete process of writing $C_{2}$ in parametric form, combining the parametric equations of $C_{1}$ and $C_{2}$ and applying $\cos ^{2} \alpha+\sin ^{2} \alpha \equiv 1$ to give an equation in one variable (i.e. $t$ ) only. |
|  | then continue with applying the mark scheme for Way 1 |
|  | Way 4 |
| M1: | Begins to solve the problem by applying an appropriate strategy. E.g. Way 4: A complete process of combining equations for $C_{1}$ and $C_{2}$ by substituting the parametric equation into the Cartesian equation to give an equation in one variable (i.e. $t$ ) only. |
| M1: <br> Note: | Uses the identities $\cos 2 t \equiv 2 \cos ^{2} t-1$ and $\cos 2 t \equiv 1-2 \sin ^{2} t$ to achieve an equation in $\cos 2 t$ only At least one of $\cos 2 t \equiv 2 \cos ^{2} t-1$ or $\cos 2 t \equiv 1-2 \sin ^{2} t$ must be correct for this mark. |
| A1: | A correct equation in $\cos 2 t$ only |
| dM1: | dependent on both the previous $M$ marks Rearranges to make $\cos 2 t=\ldots$ where $-1 \leq \cos 2 t \leq 1$ |
| M1: | See scheme |
| A1: | Selects the correct coordinates for $S$ <br> Allow either $S=(5 \sqrt{2},-4)$ or $S=($ awrt $7.07,-4)$ or $S=(\sqrt{50},-4)$ or $S=\left(\frac{10}{\sqrt{2}},-4\right)$ |



