

Question	Scheme	Marks	AOs
7	£y is the total cost of making x bars of soap Bars of soap are sold for £2 each		
(a)	$y = kx + c$ {where k and c are constants}	B1	3.3
	Note: Work for (a) cannot be recovered in (b) or (c)	(1)	
(b) Way 1	Either <ul style="list-style-type: none"> $x = 800 \Rightarrow y = 2(800) - 500 \{= 1100 \Rightarrow (x, y) = (800, 1100)\}$ $x = 300 \Rightarrow y = 2(300) + 80 \{= 680 \Rightarrow (x, y) = (300, 680)\}$ 	M1	3.1b
	Applies (800, their 1100) and (300, their 680) to give two equations $1100 = 800k + c$ and $680 = 300k + c \Rightarrow k, c = \dots$	dM1	1.1b
	Solves correctly to find $k = 0.84, c = 428$ and states $y = 0.84x + 428$ *	A1*	2.1
	Note: the answer $y = 0.84x + 428$ must be stated in (b)	(3)	
(b) Way 2	Either <ul style="list-style-type: none"> $x = 800 \Rightarrow y = 2(800) - 500 \{= 1100 \Rightarrow (x, y) = (800, 1100)\}$ $x = 300 \Rightarrow y = 2(300) + 80 \{= 680 \Rightarrow (x, y) = (300, 680)\}$ 	M1	3.1b
	Complete method for finding both $k = \dots$ and $c = \dots$ e.g. $k = \frac{1100 - 680}{800 - 300} \{= 0.84\}$ $(800, 1100) \Rightarrow 1100 = 800(0.84) + c \Rightarrow c = \dots$	dM1	1.1b
	Solves to find $k = 0.84, c = 428$ and states $y = 0.84x + 428$ *	A1*	2.1
	Note: the answer $y = 0.84x + 428$ must be stated in (b)	(3)	
(b) Way 3	Either <ul style="list-style-type: none"> $x = 800 \Rightarrow y = 2(800) - 500 \{= 1100 \Rightarrow (x, y) = (800, 1100)\}$ $x = 300 \Rightarrow y = 2(300) + 80 \{= 680 \Rightarrow (x, y) = (300, 680)\}$ 	M1	3.1b
	$\{y = 0.84x + 428 \Rightarrow\}$ $x = 800 \Rightarrow y = (0.84)(800) + 428 = 1100$ $x = 300 \Rightarrow y = (0.84)(300) + 428 = 680$	dM1	1.1b
	Hence $y = 0.84x + 428$ *	A1*	2.1
		(3)	
(c)	Allow any of {0.84, in £s} represents <ul style="list-style-type: none"> the cost of {making} each extra bar {of soap} the direct cost of {making} a bar {of soap} the marginal cost of {making} a bar {of soap} the cost of {making} a bar {of soap} (Condone this answer) Note: Do not allow <ul style="list-style-type: none"> {0.84, in £s} is the profit per bar {of soap} {0.84, in £s} is the (selling) price per bar {of soap} 	B1	3.4
		(1)	
(d) Way 1	{Let n be the least number of bars required to make a profit}		
	$2n = 0.84n + 428 \Rightarrow n = \dots$ (Condone $2x = 0.84x + 428 \Rightarrow x = \dots$)	M1	3.4
	Answer of 369 {bars}	A1	3.2a
		(2)	
(d) Way 2	<ul style="list-style-type: none"> Trial 1: $n = 368 \Rightarrow y = (0.84)(368) + 428 \Rightarrow y = 737.12$ {revenue = $2(368) = 736$ or loss = 1.12} Trial 2: $n = 369 \Rightarrow y = (0.84)(369) + 428 \Rightarrow y = 737.96$ {revenue = $2(369) = 738$ or profit = 0.04} 	M1	3.4
	leading to an answer of 369 {bars}	A1	3.2a
		(2)	
(7 marks)			

Notes for Question 7

(a)	
B1:	Obtains a correct form of the equation. E.g. $y = kx + c$; $k \neq 0, c \neq 0$. Note: Must be seen in (a)
Note:	Ignore how the constants are labelled – as long as they appear to be constants. e.g. k, c, m etc.
(b)	Way 1
M1:	Translates the problem into the model by finding either <ul style="list-style-type: none"> $y = 2(800) - 500$ for $x = 800$ $y = 2(300) + 80$ for $x = 300$
dM1:	dependent on the previous M mark See scheme
A1:	See scheme – no errors in their working
Note	Allow 1 st M1 for any of <ul style="list-style-type: none"> $1600 - y = 500$ $600 - y = -80$
(b)	Way 2
M1:	Translates the problem into the model by finding either <ul style="list-style-type: none"> $y = 2(800) - 500$ for $x = 800$ $y = 2(300) + 80$ for $x = 300$
dM1:	dependent on the previous M mark See scheme
A1:	See scheme – no error in their working
(b)	Way 3
M1:	Translates the problem into the model by finding either <ul style="list-style-type: none"> $y = 2(800) - 500$ for $x = 800$ $y = 2(300) + 80$ for $x = 300$
dM1:	dependent on the previous M mark Uses the model to test both points (800, their 1100) and (300, their 680)
A1:	Confirms $y = 0.84x + 428$ is true for both (800, 1100) and (300, 680) and gives a conclusion
Note:	Conclusion could be “ $y = 0.84x + 428$ ” or “QED” or “proved”
Note:	Give 1 st M0 for $500 = 800k + c, 80 = 300k + c \Rightarrow k = \frac{500 - 80}{800 - 300} = 0.84$
(c)	
B1:	see scheme
Note:	Also condone B1 for “rate of change of cost”, “cost of {making} a bar”, “constant of proportionality for cost per bar of soap” or “rate of increase in cost”,
Note:	Do not allow reasons such as “price increase or decrease”, “rate of change of the bar of soap” or “decrease in cost”
Note:	Give B0 for incorrect use of units. E.g. Give B0 for “the cost of making each extra bar of soap is £84” Condone the use of £0.84p

Notes for Question 7 Continued

(d) **Way 1****M1:** Using the model and constructing an argument leading to a critical value for the number of bars of soap sold. See scheme.**A1:** 369 only. Do not accept decimal answers.**(d)** **Way 2****M1:** Uses either 368 or 369 to find the cost $y = \dots$ **A1:** Attempts both trial 1 and trial 2 to find both the cost $y = \dots$ and arrives at an answer of 369 only. Do not accept decimal answers.**Note:** You can ignore inequality symbols for the method mark in part (d)**Note:** Give M1 A1 for no working leading to 369 {bars}**Note:** Give final A0 for $x > 369$ or $x > 368$ or $x \geq 369$ without $x = 369$ or 369 stated as their final answer**Note:** Condone final A1 for **in words** “at least 369 bars must be made/sold”**Note:** **Special Case:**Assuming a profit of £1 is required and achieving $x = 370$ scores special case M1A0