

<b>3(a)</b>	$2\log(4-x) = \log(4-x)^2$	B1	1.2
	$2\log(4-x) = \log(x+8) \Rightarrow \log(4-x)^2 = \log(x+8)$ $(4-x)^2 = (x+8)$ <b>or</b> $2\log(4-x) = \log(x+8) \Rightarrow \log(4-x)^2 - \log(x+8) = 0$ $\frac{(4-x)^2}{(x+8)} = 1$	M1	1.1b
	$16 - 8x + x^2 = x + 8 \Rightarrow x^2 - 9x + 8 = 0^*$	A1*	2.1
		<b>(3)</b>	
<b>(a) Alternative - working backwards:</b>			
	$x^2 - 9x + 8 = 0 \Rightarrow (4-x)^2 - x - 8 = 0$	B1	1.2
	$\Rightarrow (4-x)^2 = x + 8$ $\Rightarrow \log(4-x)^2 = \log(x+8)$	M1	1.1b
	$\Rightarrow 2\log(4-x) = \log(x+8)^*$ Hence proved.	A1	2.1
<b>(b)</b>	(i) $(x =) 1, 8$	B1	1.1b
	(ii) 8 is <b>not</b> a solution as $\log(4-8)$ cannot be found	B1	2.3
		<b>(2)</b>	
<b>(5 marks)</b>			

**Notes:**

**(a)**

**B1:** States or uses  $2\log(4-x) = \log(4-x)^2$

**M1:** Correct attempt at eliminating the logs to form a quadratic equation in  $x$ .

Note that this may be implied by e.g.  $\log \frac{(4-x)^2}{(x+8)} = 0 \Rightarrow (4-x)^2 = x+8$

**A1\*:** Proceeds to the given answer with at least one line where the  $(4-x)^2$  has been multiplied out.

There must be no errors or omissions but condone invisible brackets around the arguments of the logs e.g. allow  $\log 16 - 8x + x^2$  for  $\log(16 - 8x + x^2)$  and  $\log x + 8$  for  $\log(x + 8)$

Note we will allow a start of  $(4-x)^2 = x+8$  with no previous work for full marks.

**Some examples of how to mark (a) in particular cases:**

$$2\log(4-x) = \log(x+8) \Rightarrow \log(4-x)^2 = \log(x+8) \Rightarrow \frac{\log(4-x)^2}{\log(x+8)} = 1$$

$$2\log(4-x) = \log(x+8) \Rightarrow \log(4-x)^2 - \log(x+8) = 0 \Rightarrow (4-x)^2 - x - 8 = 0$$

$$\Rightarrow 16 - 8x + x^2 - x - 8 \Rightarrow x^2 - 9x + 8 = 0$$

**Scores B1M1A1**

$$2\log(4-x) = \log(x+8) \Rightarrow \log(4-x)^2 - \log(x+8) = 0 \Rightarrow \frac{\log(4-x)^2}{\log(x+8)} = 0$$

$$\Rightarrow \frac{(4-x)^2}{(x+8)} = 1 \Rightarrow 16 - 8x + x^2 = x + 8 \Rightarrow x^2 - 9x + 8 = 0$$

**Scores B1M0A0**

**(a) Alternative:**

**B1:** Writes  $x^2 - 9x + 8 = 0$  as  $(4-x)^2 - x - 8 = 0$  or equivalent

**M1:** Proceeds correctly to reach  $\log(4-x)^2 = \log(x+8)$

**A1:** Obtains  $2\log(4-x) = \log(x+8)$  and makes a (minimal) conclusion e.g. hence proved, QED, #, square etc.

**(b)**

**B1:** Writes down  $(x =) 1, 8$

**B1:** Chooses 8 (no follow through here) and gives a reason why it should be rejected by referring to logs and which log it is.

They must refer to the 8 as the required value but allow e.g.  $x \neq 8$  and there must be a reference to  $\log(4-x)$  or  $\log$  of lhs or  $\log(-4)$  or the  $4-8$ . Some acceptable reasons are:  $\log(-4)$  can't be found/worked out/is undefined,  $\log(-4)$  gives math error,  $\log(-4) = n/a$ , lhs is  $\log(\text{negative})$  so reject, you can't do the  $\log$  of a negative number which would happen with  $4-8$

Do **not** allow "you can't have a negative log" unless this is clarified further and do **not** allow "you get a math error" in isolation

**There must be no contradictory statements.**

Note that this is an independent mark but must have  $x = 8$  (i.e. may have solved to get  $x = -1, 8$  for first B mark)