

<b>6(a)</b>	$x^2 + 8x - 3 = (Ax + B)(x + 2) + C \text{ or } Ax(x + 2) + B(x + 2) + C$ $\Rightarrow A = \dots, B = \dots, C = \dots$ <p style="text-align: center;"><b>or</b></p> $\begin{array}{r} x+6 \\ x+2 \overline{)x^2+8x-3} \\ \underline{x^2+2x} \phantom{-3} \\ 6x-3 \\ \underline{6x+12} \\ -15 \end{array}$	M1	1.1b
	Two of $A = 1, B = 6, C = -15$	A1	1.1b
	All three of $A = 1, B = 6, C = -15$	A1	1.1b
		<b>(3)</b>	
<b>6(b)</b>	$\int \frac{x^2 + 8x - 3}{x + 2} dx = \int x + 6 - \frac{15}{x + 2} dx = \dots - 15 \ln(x + 2)$	M1	1.1b
	$= \frac{1}{2}x^2 + 6x - 15 \ln(x + 2) \quad (+c)$	A1ft	1.1b
	$\int_0^6 \frac{x^2 + 8x - 3}{x + 2} dx = \left[ \frac{1}{2}x^2 + 6x - 15 \ln(x + 2) \right]_0^6$ $= (18 + 36 - 15 \ln 8) - (0 + 0 - 15 \ln 2)$ $= 18 + 36 - (15 - 45) \ln 2 \text{ or e.g. } 18 + 36 + 15 \ln \left( \frac{2}{8} \right)$	M1	2.1
	$= 54 - 30 \ln 2$	A1	1.1b
		<b>(4)</b>	
<b>(7 marks)</b>			

**Notes:**

**(a)**

**M1:** Multiplies by  $(x + 2)$  and attempts to find values for  $A, B$  and  $C$  e.g. by comparing coefficients or substituting values for  $x$ . If the method is unclear, at least 2 terms must be correct on rhs.

**Or** attempts to divide  $x^2 + 8x - 3$  by  $x + 2$  and obtains a linear quotient and a constant remainder.

This mark may be implied by 2 correct values for  $A, B$  or  $C$

**A1:** Two of  $A = 1, B = 6, C = -15$ . But note that **just** performing the division correctly is insufficient and they must clearly identify their  $A, B, C$  to score any accuracy marks.

**A1:** All three of  $A = 1, B = 6, C = -15$

This is implied by stating  $\frac{x^2 + 8x - 3}{x + 2} = x + 6 - \frac{15}{x + 2}$  or within the integral in (b)

**(b)**

**M1:** Integrates an expression of the form  $\frac{C}{x + 2}$  to obtain  $k \ln(x + 2)$ .

Condone the omission of brackets around the “ $x + 2$ ”

**A1ft:** Correct integration ft on their  $Ax + B + \frac{C}{x + 2}$ , ( $A, B, C \neq 0$ ) The brackets should be present around the “ $x + 2$ ” unless they are implied by subsequent work.

**M1:** Substitutes both limits 0 and 6 into an expression that contains an  $x$  or  $x^2$  term or both and a  $\ln$  term and subtracts either way round **WITH** fully correct log work to combine two log terms (but allow sign errors when removing brackets) leading to an answer of the form  $a + b \ln c$  ( $a, b$  and  $c$  not necessarily integers) e.g. if they expand to get  $-15 \ln 8 - 15 \ln 2$  followed by  $-15 \ln 16$  and reach  $a + b \ln c$  then allow the M mark

**A1:**  $54 - 30 \ln 2$  (Apply isw once a correct answer is seen)