

14. A circle  $C$  with radius  $r$

- lies only in the 1st quadrant
- touches the  $x$ -axis and touches the  $y$ -axis

The line  $l$  has equation  $2x + y = 12$

(a) Show that the  $x$  coordinates of the points of intersection of  $l$  with  $C$  satisfy

$$5x^2 + (2r - 48)x + (r^2 - 24r + 144) = 0$$

(3)

Given also that  $l$  is a tangent to  $C$ ,

(b) find the two possible values of  $r$ , giving your answers as fully simplified surds.

(4)