

Question	Scheme	Marks	AOs
9	$a = \left(\frac{3}{4}\right)^2 \text{ or } a = \frac{9}{16}$ <p style="text-align: center;">or</p> $r = -\frac{3}{4}$	B1	2.2a
	$\sum_{n=2}^{\infty} \left(\frac{3}{4}\right)^n \cos(180n)^\circ = \frac{\frac{9}{16}}{1 - \left(-\frac{3}{4}\right)} = \dots$	M1	3.1a
	$= \frac{9}{28}^*$	A1*	1.1b
	<b>(3)</b>		
<b>Alternative 1:</b>			
	$\sum_{n=1}^{\infty} \left(\frac{3}{4}\right)^n \cos(180n)^\circ = \frac{-\frac{3}{4}}{1 - \left(-\frac{3}{4}\right)} = \dots \text{ or } r = -\frac{3}{4}$	B1	2.2a
	$\sum_{n=2}^{\infty} \left(\frac{3}{4}\right)^n \cos(180n)^\circ = -\frac{3}{7} - \left(-\frac{3}{4}\right)$	M1	3.1a
	$= \frac{9}{28}^*$	A1*	1.1b
<b>Alternative 2:</b>			
	$\sum_{n=2}^{\infty} \left(\frac{3}{4}\right)^n \cos(180n)^\circ = \left(\frac{3}{4}\right)^2 - \left(\frac{3}{4}\right)^3 + \left(\frac{3}{4}\right)^4 - \dots$	B1	2.2a
	$= \left(\frac{3}{4}\right)^2 + \left(\frac{3}{4}\right)^4 + \dots - \left(\frac{3}{4}\right)^3 - \left(\frac{3}{4}\right)^5 - \dots$ $\left(\frac{3}{4}\right)^2 + \left(\frac{3}{4}\right)^4 + \dots = \left(\frac{3}{4}\right)^2 \left(\frac{1}{1 - \left(\frac{3}{4}\right)^2}\right) \text{ or } -\left(\frac{3}{4}\right)^3 - \left(\frac{3}{4}\right)^5 - \dots = -\left(\frac{3}{4}\right)^3 \left(\frac{1}{1 - \left(\frac{3}{4}\right)^2}\right)$ $\sum_{n=2}^{\infty} \left(\frac{3}{4}\right)^n \cos(180n)^\circ = \left(\frac{3}{4}\right)^2 \left(\frac{1}{1 - \left(\frac{3}{4}\right)^2}\right) - \left(\frac{3}{4}\right)^3 \left(\frac{1}{1 - \left(\frac{3}{4}\right)^2}\right)$	M1	3.1a
	$= \frac{9}{28}^*$	A1*	1.1b
<b>Alternative 3:</b>			
	$\sum_{n=2}^{\infty} \left(\frac{3}{4}\right)^n \cos(180n)^\circ = S = \left(\frac{3}{4}\right)^2 - \left(\frac{3}{4}\right)^3 + \left(\frac{3}{4}\right)^4 - \dots$	B1	2.2a
	$= \left(\frac{3}{4}\right)^2 \left(1 - \left(\frac{3}{4}\right) + \left(\frac{3}{4}\right)^2 - \dots\right) = \left(\frac{3}{4}\right)^2 \left(\frac{1}{4} + S\right) \Rightarrow \frac{7}{16}S = \frac{9}{64} \Rightarrow S = \dots$	M1	3.1a
	$= \frac{9}{28}^*$	A1*	1.1b
<b>(3 marks)</b>			
<b>Notes</b>			

B1: Deduces the correct value of the **first** term or the common ratio. The correct first term can be seen as part of them writing down the sequence but must be the **first** term.

M1: Recognises that the series is infinite geometric and applies the sum to infinity GP formula

with  $a = \frac{9}{16}$  and  $r = \pm \frac{3}{4}$

A1\*: Correct proof

**Alternative 1:**

B1: Deduces the correct value for the sum to infinity (starting at  $n = 1$ ) or the common ratio

M1: Calculates the required value by subtracting the first term from their sum to infinity

A1\*: Correct proof

**Alternative 2:**

B1: Deduces the correct value of the **first** term or the common ratio.

M1: Splits the series into “odds” and “evens”, attempts the sum of both parts and calculates the required value by adding both sums

A1\*: Correct proof

**Alternative 3:**

B1: Deduces the correct value of the **first** term

M1: A complete method by taking out the first term, expresses the rhs in terms of the original sum and rearranges for “S”

A1\*: Correct proof