

Question	Scheme	Marks	AOs
14(a)	$u = 1 + \sin^2 x \Rightarrow \frac{du}{dx} = 2 \sin x \cos x$	B1	1.1b
	$\int \frac{8 \tan x}{1 + \sin^2 x} dx = \int \frac{8 \tan x}{u} \frac{du}{2 \sin x \cos x}$	M1	2.1
	$= \int \frac{4}{u \cos^2 x} du = \int \frac{4}{u(1 - \sin^2 x)} du = \int \frac{4}{u(1 - (u-1))} du$	M1	3.1a
	$= \int \frac{4}{u(2-u)} du *$	A1*	2.1
	$p=1 \text{ and } q=\frac{5}{4}$	B1	2.2a
		(5)	
(b)	$\frac{4}{u(2-u)} \equiv \frac{a}{u} + \frac{b}{2-u} \Rightarrow a = \dots, b = \dots$	M1	2.1
	$\frac{4}{u(2-u)} \equiv \frac{2}{u} + \frac{2}{2-u}$	A1	1.1b
	$= \int \frac{4}{u(2-u)} du = 2 \ln u - 2 \ln(2-u) (+c)$	dM1 A1ft	3.1a 1.1b
	$= \int_1^{\frac{5}{4}} \frac{4}{u(2-u)} du = [2 \ln u - 2 \ln(2-u)]_1^{\frac{5}{4}} = 2 \ln \frac{5}{4} - 2 \ln \left(2 - \frac{5}{4}\right) - (0)$	M1	1.1b
	$= \ln \frac{25}{9}$	A1	2.1
		(6)	

(11 marks)