Question	Scheme	Marks	AOs
3 (a)	h = 0.3	B1	1.1a
	$A \approx \frac{0.3}{2} \left\{ 1.811 + 2.944 + 2 \left(2.342 + 2.718 + 2.941 + 3.011 \right) \right\}$	M1	1.1b
	= 4.02	A1	1.1b
		(3)	
(b)	Underestimate and a relevant justification e.g.		
	• {top of} trapezia lie below the curve		
	• Area of trapezia < area under curve		
	• An appropriate diagram which gives reference to the lost area	B1	3.2b
	• Curve is concave		
	• The gradient of the curve is {continually} decreasing		
		(1)	
(c)	$\int_{-0.6}^{0.9} (8 - 2f(x)) dx = \dots - 2 \times "4.02"$	M1	1.1b
	$\int_{-0.6}^{0.9} (8 - 2f(x)) dx = 8 \times 1.5 - \dots$	M1	3.1a
	$\int_{-0.6}^{0.9} (8 - 2f(x)) dx = 8 \times 1.5 - 2 \times "4.02" = 3.96$	Alft	2.2a
		(3)	
			marks)
Notes			
(a) B1: States or uses $h = 0.3$ M1: Correct attempt at the trapezium rule. Must be an attempt at the correct structure e.g.			
$\frac{h}{2} \{ y_{-0.6} + y_{0.3} + 2(y_0 + y_{0.3} + y_{0.6} + y_{0.9}) \}$ with brackets as shown unless they are implied by			
subsequent work			
A1: For awrt 4.02			
B1: see main scheme (c)			
M1: For multiplying their answer to part (a) by ± 2			
$\frac{1}{2}$			

M1: For a correct strategy for the "8" part of the integral. May see e.g. 8×1.5 or $8 \times (0.9 + 0.6)$ or $\int_{0.9}^{0.9} 8 \, dr = [8r]^{0.9} = 8 \times 0.9 = 8 \times (-0.6)$

$$\int_{-0.6}^{0.9} 8 \, dx = \left[8x \right]_{-0.6}^{0.9} = 8 \times 0.9 - 8 \times (-0.6)$$

A1ft: For awrt 3.96 (or 3.97 if full accuracy used from (a)) or follow through $12 - 2 \times$ their answer to part (a)