

Question	Scheme	Marks	AOs
8(a)	$R = \sqrt{2^2 + 8^2} = \sqrt{68} = 2\sqrt{17}$	<b>B1</b>	1.1b
	$2 \cos \theta + 8 \sin \theta = R \cos \theta \cos \alpha + R \sin \theta \sin \alpha$ $2 = R \cos \alpha \quad 8 = R \sin \alpha$ $\tan \alpha = \frac{8}{2} \Rightarrow \alpha = \dots$	<b>M1</b>	1.1b
	$\alpha = \text{awrt } 1.326$	<b>A1</b>	2.2a
		<b>(3)</b>	
(b)(i)	$4.5 \times "2\sqrt{17}"$	<b>M1</b>	1.1b
	$9\sqrt{17}$	<b>A1</b>	2.2a
(ii)	awrt 1.33	<b>B1ft</b>	2.2a
		<b>(3)</b>	

**(6 marks)**

### Notes

**(a)**

**B1:**  $R = 2\sqrt{17}$  or  $\sqrt{68}$ .

$\pm 2\sqrt{17}$  or  $\pm\sqrt{68}$  score B0

(Condone if this comes from e.g.,  $8 = R \cos \alpha \quad 2 = R \sin \alpha$ )

Decimal answers score B0 unless the exact value is seen then apply isw.

**M1:** Proceeds to a value for  $\alpha$  from  $\tan \alpha = \pm \frac{8}{2}$ ,  $\cos \alpha = \pm \frac{2}{\sqrt{68}}$ ,  $\sin \alpha = \pm \frac{8}{\sqrt{68}}$

May be implied by awrt 1.33 radians or 76 degrees

**A1:** awrt 1.326 for  $\alpha$ . Apply isw if this is then subsequently rounded to e.g. 1.33

**(b)(i)**

**M1:** For a value of  $\pm 4.5 \times$  their  $R$  or allow  $\pm 4.5R$  (with the letter  $R$ )

But not embedded in an expression e.g.  $9\sqrt{17} \cos(\theta - \alpha)$  unless extracted later.

Note that the sum may be found as  $9 \cos x + 36 \sin x$  with the maximum then found using calculus

e.g.  $S = 9 \cos x + 36 \sin x \Rightarrow \frac{dS}{dx} = -9 \sin x + 36 \cos x = 0 \Rightarrow \tan x = 4 \Rightarrow \sin x = \frac{4}{\sqrt{17}}$ ,  $\cos x = \frac{1}{\sqrt{17}}$

$\Rightarrow 9 \cos x + 36 \sin x = 9\sqrt{17}$ . This will score M1 once they reach  $\pm 4.5 \times$  their  $R$

May be implied by  $9\sqrt{17}$  or awrt 37.1 (which may come from a graphical method)

May also see e.g.  $\text{Max}(9 \cos x + 36 \sin x) = \sqrt{9^2 + 36^2} = \dots$

**A1:**  $9\sqrt{17}$  or exact equivalent e.g.  $\sqrt{1377}$ ,  $4.5\sqrt{68}$ ,  $4.5(2\sqrt{17})$  and apply isw once a correct answer is seen

**(ii)**

**B1ft:** awrt 1.33 (or follow through on their  $\alpha$  even if in degrees (76), no matter how accurate)