

| Question | Scheme | Marks | AOs |
|--------------|--|-------------|------|
| 10(a) | e.g. $\frac{3kx-18}{(x+4)(x-2)} \equiv \frac{A}{x+4} + \frac{B}{x-2} \Rightarrow 3kx-18 \equiv A(x-2) + B(x+4)$ or $\frac{3kx-18}{(x+4)(x-2)} \equiv \frac{A}{x-2} + \frac{B}{x+4} \Rightarrow 3kx-18 \equiv A(x+4) + B(x-2)$ | B1 | 1.1b |
| | $6k-18=6B \Rightarrow B=...$ or $-12k-18=-6A \Rightarrow A=...$ or $3kx-18 \equiv (A+B)x + 4B - 2A \Rightarrow A+B=3k, -18=4B-2A$ $\Rightarrow A=...$ or $B=...$ | M1 | 1.1b |
| | $\frac{2k+3}{x+4} + \frac{k-3}{x-2}$ | A1 | 1.1b |
| | (3) | | |
| (b) | $\int \left(\frac{"2k+3"}{x+4} + \frac{"k-3"}{x-2} \right) dx = ... \ln(x+4) + ... \ln(x-2)$ | M1 | 1.2 |
| | $("2k+3") \ln(x+4) + ("k-3") \ln(x-2)$ | A1ft | 1.1b |
| | $("2k+3") \ln(5) - ("k-3") \ln(5) \Rightarrow ("k+6") \ln 5 = 21 \Rightarrow k=...$ | dM1 | 3.1a |
| | $(k=) \frac{21}{\ln 5} - 6$ | A1 | 2.2a |
| | (4) | | |

(7 marks)

Notes

(a)

B1: Correct form for the partial fractions and sets up the correct corresponding identity which may be implied by two equations in A and B if they are comparing coefficients.

M1: Either

- substitutes $x=2$ or $x=-4$ in an attempt to find A or B in terms of k
- expands the rhs, collects terms and compares coefficients in an attempt to find A or B in terms of k

Or may be implied by one correct fraction (numerator **and** denominator)

You may see candidates substituting two other values of x and then solving simultaneous equations.

A1: Achieves $\frac{2k+3}{x+4} + \frac{k-3}{x-2}$ with no errors. Must be the correct partial fractions not just for correct

numerators. May be seen in (b). Correct answer implies B1M1A1. One correct fraction only B0M1A0

(b)

M1: Attempts to find $\int \left(\frac{"2k+3"}{x+4} + \frac{"k-3"}{x-2} \right) dx$. Score for either $\frac{\dots}{x+4} \rightarrow \dots \ln(x+4)$ or $\frac{\dots}{x-2} \rightarrow \dots \ln(x-2)$

Allow the ... to be in terms of k or just constants but there must be no x terms.

Condone invisible brackets for this mark.

A1ft: ("2k+3")ln|x+4|+("k-3")ln|x-2|

but condone round brackets e.g. ("2k+3")ln(x+4)+("k-3")ln(x-2) or equivalent e.g.

("2k+3")ln(x+4)+("k-3")ln(2-x)

Follow through their partial fractions with numerators which must both be in terms of k .

Condone missing brackets as long as they are recovered later e.g. when applying limits.

dm1: A full attempt to find the value of k . To score this mark they must have attempted to integrate their partial fractions, substituted in the correct limits, subtracted either way round, set = 21 and attempted to solve to find k . Condone omission of the terms containing ln(1) or ln(-1).

Note that e.g. ln(-5) or ln(5) must be seen but may be disregarded **after** substitution and subtraction.

Do not be concerned with the processing as long as they proceed to $k = \dots$

Condone if they use x instead of k after limits have been used as long as the intention is clear.

A1: Deduces $(k =) \frac{21}{\ln 5} - 6$ or exact equivalent e.g. $\frac{21-6\ln 5}{\ln 5}$, $\frac{21-3\ln 25}{\ln 5}$.

Allow recovery from expressions that contain e.g. ln(-5) as long as it is dealt with subsequently.

Also allow recovery from invisible brackets. Condone $x = \frac{21}{\ln 5} - 6$

Some candidates may use substitution in part (b) e.g.

$$\int \left(\frac{"2k+3"}{x+4} + \frac{"k-3"}{x-2} \right) dx = \int \left(\frac{"2k+3"}{x+4} \right) dx + \int \left(\frac{"k-3"}{x-2} \right) dx$$

$$u = x+4 \Rightarrow \int \left(\frac{"2k+3"}{x+4} \right) dx = \int \left(\frac{"2k+3"}{u} \right) du = \dots \ln u$$

$$u = x-2 \Rightarrow \int \left(\frac{"k-3"}{x-2} \right) dx = \int \left(\frac{"k-3"}{u} \right) du = \dots \ln u$$

Score **M1** for integrating at least once to an appropriate form as in the main scheme e.g. ...lnu

A1ft: For ("2k+3")ln|u|+("k-3")ln|u|

but condone ("2k+3")ln u + ("k-3")ln u which may be seen separately

Follow through their "A" and "B" in terms of k .

Condone missing brackets as long as they are recovered later e.g. when applying limits.

dm1: A full attempt to find the value of k . To score this mark they must have attempted to integrate their partial fractions using substitution, substituted in the correct changed limits and subtracts either way

round, set = 21 and attempted to solve to find k . Do not be concerned with processing as long as they proceed to $k = \dots$. Condone omission of terms which contain e.g. $\ln(1)$ or $\ln(-1)$.

Note that e.g. $\ln(-5)$ or $\ln(5)$ must be seen but may be disregarded **after** substitution and subtraction.

$$[(2k + 3) \ln u]_1^5 + [(k - 3) \ln u]_{-5}^{-1} = 21 \Rightarrow (2k + 3) \ln 5 - (2k + 3) \ln 1 + (k - 3) \ln 1 - (k - 3) \ln 5 = 21$$

$$\Rightarrow (2k + 3) \ln 5 - (k - 3) \ln 5 = 21 \Rightarrow (k + 6) \ln 5 = 21 \Rightarrow k = \dots$$

A1: $k = \frac{21}{\ln 5} - 6$ or exact equivalent e.g. $\frac{21 - 6 \ln 5}{\ln 5}$, $\frac{21 - 3 \ln 25}{\ln 5}$, $21 \log_5 e - 6$.

Allow recovery from expressions that contain e.g. $\ln(-5)$ as long as it is dealt with subsequently.

Also allow recovery from invisible brackets.