

Question	Scheme	Marks	AOs
<b>5(a)</b>	$-3 = \frac{t-1}{2} \Rightarrow t = -5 \Rightarrow y = 5(" - 5 " + 2)^4$	M1	1.1b
	$(y =) 405$	A1	1.1b
		<b>(2)</b>	
<b>(b)</b>	$x = \frac{t-1}{2} \Rightarrow t = 2x+1 \Rightarrow y = 5(" 2x+1 " + 2)^4$	M1	1.1b
	$y = 5(2x+3)^4$	A1	1.1b
		<b>(2)</b>	
<b>(c)</b>	$(" 2x+3 ")^n \rightarrow ... (" 2x+3 ")^{n-1}$	M1	1.1b
	$\left(\frac{dy}{dx} = \right) 40(2(-3)+3)^3$	dM1	1.1b
	$\left(\frac{dy}{dx} = \right) -1080$	A1	1.1b
		<b>(3)</b>	

(7 marks)

Notes	
<b>(a)</b>	<b>Mark parts (a) and (b) together.</b>
M1:	Substitutes $x = -3$ into $x = \frac{t-1}{2}$ , attempts to find $t$ , and substitutes their $t$ into $y = 5(t+2)^4$ Condone slips. May be implied by substitution of $t = -5$ into $y$ or by 405 or by $y = 5(-3)^4$ Alternatively, they may substitute $x = -3$ into their $y = f(x)$
A1:	cao Answer only scores full marks and ISW after seeing 405 e.g. $(-5, 405)$ Accept $(-3, 405)$ or e.g. $P = 405$
<b>(b)</b>	<b>Mark parts (a) and (b) together.</b>
M1:	Attempts to make $t$ the subject of $x = \frac{t-1}{2}$ using the correct <b>order</b> of operations and substitutes into $y = 5(t+2)^4$ Condone slips e.g. dividing by 2 first: $t = \frac{x}{2} + 1$ or missing the +2 in $y = 5(t+2)^4$
<b>Alt 1:</b>	Writes $t = \left(\frac{y}{5}\right)^{\frac{1}{4}} - 2$ , substitutes into $x = \frac{t-1}{2}$ and attempts to make $y$ the subject using the correct <b>order</b> of operations, i.e., $2x = \left(\frac{y}{5}\right)^{\frac{1}{4}} - 3 \Rightarrow (2x+3)^4 = \frac{y}{5} \Rightarrow y = 5(2x+3)^4$
<b>Alt 2:</b>	Makes $t$ the subject and then substitutes into an expanded $5(t+2)^4$ Do not be too concerned about their expansion, but it must contain $t^4$ and a constant term.
A1:	cao and ISW after a correct answer seen. May be scored for $y = 5(2x+1+2)^4$ Allow e.g. $y = 80x^4 + 480x^3 + 1080x^2 + 1080x + 405$ or e.g. $y = 5(2x+1)^4 + 40(2x+1)^3 + 120(2x+1)^2 + 160(2x+1) + 80$ Their RHS may be unsimplified but do not allow if e.g. binomial coefficients are still present. Do not accept $f(x) = \dots$ It must be $y = \dots$

(c) **Note: Differentiation seen in (a) or (b) can score marks if used in (c)**

M1: Reduces the power of their  $(2x+3)^n$  by one to  $Q(2x+3)^{n-1}$  where  $Q$  is a constant and could be 1. There should be no other terms using this method.

Alternatively, attempts to expand their  $(2x+3)^n$  (may have been expanded in (b)) and reduces the power of  $x$  by one in at least one term.

They may use parametric differentiation, i.e.,  $\frac{dy}{dt} = a(t+2)^3$  and  $\frac{dx}{dt} = b$  where  $a$  and  $b$  are

constants, leading to  $\frac{dy}{dx} = \frac{a(t+2)^3}{b}$  i.e. they must divide the correct way round.

Condone attempts at the chain rule that reach e.g.  $y' = \dots u^3$  but make a slip when substituting back in for  $x$  or  $t$ , e.g.,  $\frac{dy}{dx} = (5x+3)^3$  or  $\frac{dy}{dt} = (t+2)^2$ , provided the intention is clear.

dM1: Substitutes  $x = -3$  into their  $\frac{dy}{dx}$  in terms of  $x$  which may be implied by their answer.

Using parametric differentiation, substitutes their  $t$  (found from an attempt at substituting  $x = -3$  into  $x = \frac{t-1}{2}$  which may have been seen in (a)) into their  $\frac{dy}{dx}$  in terms of  $t$ .

Note for reference, if correct, the parametric differentiation is  $\frac{dy}{dt} = 20(t+2)^3$  and  $\frac{dx}{dt} = \frac{1}{2}$

leading to  $\frac{dy}{dx} = 40(t+2)^3$

They may substitute their value of  $t$  into  $\frac{dy}{dt}$  first before using the chain rule to reach  $\frac{dy}{dx}$  which is acceptable and implies the first M mark.

A1:  $\left(\frac{dy}{dx} = \right) -1080$

Correct answer only scores full marks.

May be seen labelled as  $m$  or something else.