

3. In an experiment a group of children each repeatedly throw a dart at a target. For each child, the random variable H represents the number of times the dart hits the target in the first 10 throws.

Peta models H as $B(10, 0.1)$

(a) State two assumptions Peta needs to make to use her model. (2)

(b) Using Peta’s model, find $P(H \geq 4)$ (1)

For each child the random variable F represents the number of the throw on which the dart first hits the target.

Using Peta’s assumptions about this experiment,

(c) find $P(F = 5)$ (2)

Thomas assumes that in this experiment no child will need more than 10 throws for the dart to hit the target for the first time. He models $P(F = n)$ as

$$P(F = n) = 0.01 + (n - 1) \times \alpha$$

where α is a constant.

(d) Find the value of α (4)

(e) Using Thomas’ model, find $P(F = 5)$ (1)

(f) Explain how Peta’s and Thomas’ models differ in describing the probability that a dart hits the target in this experiment. (1)