

| Question  |           | Answer                    | Mks  | AO   | Guidance                                  |                           |
|---|-----------|---------------------------|--|--|---|---------------------------|
| 5   |           | $N = 3k + 1$              | <b>M1</b>  | <b>3.1a</b>  | <b>One</b> of these. Allow without "N = " | Any letter other than $p$ |
|   |           | or $N = 3k + 2$           |  |  |   |                           |
|   |           | (where $k$ is an integer) | <b>M1</b>  | <b>1.1</b>   | Attempt <b>one</b> of these               | Allow $p$                 |
|   |           | $(3k + 1)^2$              |  |  |   |                           |
|   |           | $= 9k^2 + 6k + 1$         | <b>A1</b>  | <b>2.1</b>   | <b>Both</b> correct                       | Allow $p$                 |
| $= 3(3k^2 + 2k) + 1$ or $= 3(3k^2 + 4k + 1) + 1$        | <b>A1</b> | <b>2.4</b>                | Or $9k^2 + 6k$ div by 3 or $9k^2 + 12k + 3$ div by 3   | or similar in words. Allow $p$                             |   |                           |
| <b>Both</b> these are of form $3p + 1$ , $p$ an integer | <b>E1</b> | <b>2.2a</b>               | <b>One</b> of these<br>Must say $p$ is integer or $3k^2 + 2k$ and $3k^2 + 4k + 1$ are integers | Dep on M1M1A1A1  |   |                           |
|   |           |                           |  | Similar marks for method using $N = 3k + 1$ & $N = 3k - 1$ | $N = 3p + 1$ : max M0M1A1A1E0             |                           |
|   |           |                           | <b>[5]</b>   |  |   |                           |