$$
\begin{equation*}
x^{2}+(m x)^{2}-6 x-2 m x+5=0 \tag{I}
\end{equation*}
$$

$\left(1+m^{2}\right) x^{2}-(6+2 m) x+5=0$
$(6+2 m)^{2}-20\left(1+m^{2}\right) \quad(\geq 0)$
$\Delta=-16 m^{2}+24 m+16 \quad(\geq 0)$
Roots of $-16 m^{2}+24 m+16=0$ are $m=2$ and $m=-\frac{1}{2}$
Range for real solutions is $-\frac{1}{2} \leq m \leq 2$

| Question |  | Answer | Marks | AO | Guidance |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 7 | (b) | $m=2 \Rightarrow x^{2}+4 x^{2}-6 x-4 x+5=0 \quad\left(\Rightarrow 5 x^{2}-10 x+5=0\right)$ <br> $x=1, \&$ repeated root or only one root oe or $x=1, x=1$ <br> NB May be implied by next line. <br> Line is a tangent | $\begin{gathered} \text { M1 } \\ \text { A1 } \\ \text { A1 } \end{gathered}$ | 1.1 <br> 2.1 | Substitute $m=2$ into their (I) or substitute $y=2 x$ into $x^{2}+y^{2}-6 x-2 y+5=0$ <br> or "Only one intersection point" oe dep M1 only |
|  |  | Alternative method 1 <br> $m=2$ gives $\Delta=-16 \times 2^{2}+24 \times 2+16$ <br> $=0$. hence repeated root or only one root oe <br> NB May be implied by next line. <br> Line is a tangent | $\begin{array}{r} \text { M1 } \\ \text { A1 } \\ \mathbf{A 1} \\ \hline \end{array}$ |  | Substitute $m=2$ into their $\Delta$ <br> or "Only one intersection point" oe |
|  |  | Alternative method 2 <br> Attempt draw circle centre $(3,1)$ and line through $O$ Approximately correct diagram showing line touching circle State "Tangent" or "Only one intersection point" oe | $\begin{array}{r} \text { M1 } \\ \text { A1 } \\ \text { A1 } \\ \hline \end{array}$ |  | NB Question allows for diagrammatic solution. <br> Dep M1A1 |
|  |  |  | [3] |  | . |

