

Question			Answer	Mark	AO	Guidance
7	(a)	(i)	$\frac{a^2+b^2}{2}, \left(\frac{a+b}{2}\right)^2$	<b>B1</b> <b>[1]</b>	<b>1.1</b>	Both oe (NOT $\frac{(a+b)^2}{2}$ ) isw any multiplying out in this part
7	(a)	(ii)	$\frac{a^2+b^2}{2} - \left(\frac{a+b}{2}\right)^2$  $= \frac{2a^2+2b^2-(a^2+2ab+b^2)}{4}$  $= \frac{(a-b)^2}{4} \geq 0$	<b>M1*</b>  <b>dM1</b>  <b>A1</b>	<b>3.1a</b>  <b>1.1</b>  <b>2.2a</b>	Difference between two expressions from <b>(a)(i)</b>  oe, attempt collect over denominator of 4  Must see $\frac{(a-b)^2}{4}$ and " $\geq 0$ "
			<b>Alternative method:</b> $\left(\frac{a+b}{2}\right)^2 = \frac{a^2+2ab+b^2}{4}$  For the statement to be true: $\frac{a^2+b^2}{2} \geq \frac{a^2+2ab+b^2}{4}$ $2a^2+2b^2 \geq a^2+2ab+b^2$ $a^2+b^2 \geq 2ab$ $a^2+b^2-2ab \geq 0$  Which is true because $(a-b)^2 \geq 0$	<b>M1*</b>  <b>dM1</b>  <b>A1</b>  <b>[3]</b>		Multiplying out their expression for the square of the mean of the form $(c+d)^2$ to reach $c^2+2cd+d^2$ (need not include the denominator). May be seen in part (a)(i). If two such expressions are present they must both be correctly multiplied out.  Comparing their two expressions (condone <, >, = but expressions must be of the correct form i.e. not $\Sigma$ ) and attempting to manipulate (must include denominators)  (for any real values of $a$ and $b$ ) Must see this or an equivalent statement
7	(b)		Variance is $\geq 0$	<b>B1</b>  <b>[1]</b>	<b>3.2a</b>	Condone Variance is positive or 'never negative' (because Variance is the difference between the mean of the squares and the square of the mean)