

11	(a)	(i)	$\left(\frac{3}{25}\right)^2 \times \frac{1}{5}$ $(\times 3)$ $= \frac{27}{3125}$ or 0.00864 ISW	M1	3.1a	Correct product seen, not necessarily alone. Allow without "× 3" May be implied by the answer
				A1	1.1	NB $\left(\frac{1}{5}\right)^3 = 0.008$ M0A0
				[2]		
11	(a)	(ii)	$\left(\frac{3}{25}\right)^2 \times \frac{22}{25} + \left(\frac{1}{5}\right)^2 \times \frac{4}{5} + \left(\frac{8}{25}\right)^2 \times \frac{17}{25} + \left(\frac{7}{25}\right)^2 \times \frac{18}{25} + \left(\frac{2}{25}\right)^2 \times \frac{23}{25}$ or 0.0127 + 0.032 + 0.0696 + 0.0564 + 0.00589 or $\frac{198}{15625} + \frac{4}{125} + \frac{1088}{15625} + \frac{882}{15625} + \frac{92}{15625}$ = 0.177 (3 sf) or $\frac{552}{3125}$ or $\frac{2760}{15625}$	M1 M1	3.4 1.1	M2 for all 5 correct products M1 for 2 correct products
				A1	1.1	Correct answer with no working scores M1M0A1 SC. If no marks scored, but all 20 cases listed: B1
			Alternative method. P(1 st 2 the same) – P(all 3 same) $\left(\frac{3}{25}\right)^2 + \left(\frac{1}{5}\right)^2 + \left(\frac{8}{25}\right)^2 + \left(\frac{7}{25}\right)^2 + \left(\frac{2}{25}\right)^2$ $- \left(\left(\frac{3}{25}\right)^3 + \left(\frac{1}{5}\right)^3 + \left(\frac{8}{25}\right)^3 + \left(\frac{7}{25}\right)^3 + \left(\frac{2}{25}\right)^3\right)$ = 0.177 (3 sf) or $\frac{552}{3125}$	M2 A1		M1 for either P(1 st 2 the same) or P(all 3 same) correct

Question			Answer	Marks	AO	Guidance
			<p>Alternative method using 20 cases</p> $\left(\frac{3}{25}\right)^2 \times \frac{1}{5} + \left(\frac{3}{25}\right)^2 \times \frac{8}{25} + \left(\frac{3}{25}\right)^2 \times \frac{7}{25} + \left(\frac{3}{25}\right)^2 \times \frac{2}{25}$ <p>or $0.00288 + 0.004608 + 0.004032 + 0.001152$</p> $\text{or } + \frac{45}{15625} + \frac{72}{15625} + \frac{63}{15625} + \frac{18}{15625}$ $+ \left(\frac{1}{5}\right)^2 \times \frac{3}{25} + \left(\frac{1}{5}\right)^2 \times \frac{8}{25} + \left(\frac{1}{5}\right)^2 \times \frac{7}{25} + \left(\frac{1}{5}\right)^2 \times \frac{2}{25}$ <p>or $+ 0.0048 + 0.0128 + 0.0112 + 0.0032$</p> $\text{or } \frac{3}{625} + \frac{8}{625} + \frac{7}{625} + \frac{2}{625}$ $+ \left(\frac{8}{25}\right)^2 \times \frac{3}{25} + \left(\frac{8}{25}\right)^2 \times \frac{1}{5} + \left(\frac{8}{25}\right)^2 \times \frac{7}{25} + \left(\frac{8}{25}\right)^2 \times \frac{2}{25}$ <p>or $+ 0.01229 + 0.0205 + 0.0287 + 0.00819$</p> $\text{or } + \frac{192}{15625} + \frac{64}{3125} + \frac{448}{15625} + \frac{128}{15625}$ $+ \left(\frac{7}{25}\right)^2 \times \frac{3}{25} + \left(\frac{7}{25}\right)^2 \times \frac{1}{5} + \left(\frac{7}{25}\right)^2 \times \frac{8}{25} + \left(\frac{7}{25}\right)^2 \times \frac{2}{25}$ <p>or $+ 0.00941 + 0.0157 + 0.0251 + 0.00627$</p> $\text{or } \frac{147}{15625} + \frac{49}{3125} + \frac{392}{15625} + \frac{98}{15625}$ $+ \left(\frac{2}{25}\right)^2 \times \frac{3}{25} + \left(\frac{2}{25}\right)^2 \times \frac{1}{5} + \left(\frac{2}{25}\right)^2 \times \frac{8}{25} + \left(\frac{2}{25}\right)^2 \times \frac{7}{25}$ <p>or $0.000768 + 0.00128 + 0.00205 + 0.00179$</p> $\text{or } \frac{12}{15625} + \frac{4}{3125} + \frac{32}{15625} + \frac{28}{15625}$ <p>$= 0.177 \text{ (3 sf) or } \frac{552}{3125}$</p>	A1		<p>M2 for all 20 products</p> <p>M1 for 8 correct products</p>
				[3]		

Question		Answer	Marks	AO	Guidance
11	(b)	<p>Basic scheme: Must refer to some aspect of the model that makes ≈ 3 goals per match unlikely</p> <p>Must mention or imply ≈ 3 goals per match</p> <p>EG:</p> <p>Current model seems to underestimate probabilities of higher numbers of goals</p> <p>Or about 3 goals per match, but mean in the model is < 3</p> <p>Or about 3 goals per match, but mean = 2 or median = 2</p> <p>Or model suggests more matches $<$ than 3 than > 3</p> <p>Or model suggests < 3 goals per match</p>	B1	3.5a	<p>oe. Or eg $P(X > 4)$ should be more than 0</p> <p>or model suggests impossible to score more than 4 goals</p> <p>or model says $P(3 \text{ or more}) = 0.36$ which is small</p> <p>NOT ≈ 3 goals per match, but $P(X = 3) = \frac{7}{25}$, too small.</p> <p>NOT ≈ 3 goals per match, but $(\frac{7}{25})^{10}$ is tiny</p> <p>NOT ≈ 3 goals per match unlikely given this model</p> <p>NOT 3 is not the most likely number of goals</p> <p>NOT Highest probability is 2</p> <p>Ignore all else</p>
			[1]		