

7	(a)	$\overline{AB} = \overline{OB} - \overline{OA} = (4\mathbf{i} - 3\mathbf{j}) - (2\mathbf{i} + 4\mathbf{j}) (= 2\mathbf{i} - 7\mathbf{j})$ $\sqrt{53} \text{ or } 53 \text{ from } \pm(2\mathbf{i} - 7\mathbf{j})$ $ \overline{OA}  = \sqrt{20}, \quad  \overline{OB}  = 5$ $\cos AOB = \frac{(\sqrt{20})^2 + 5^2 - (\sqrt{53})^2}{2(\sqrt{20})(5)}$ $\cos AOB = \left( \frac{20 + 25 - 53}{10\sqrt{20}} = \right) - \frac{4}{5(2\sqrt{5})} = -\frac{2\sqrt{5}}{25}$	<p><b>M1</b></p> <p><b>A1</b></p> <p><b>B1</b></p> <p><b>M1</b></p> <p><b>A1</b></p>	<p><b>2.1</b></p> <p><b>1.1</b></p> <p><b>1.1</b></p> <p><b>3.1a</b></p> <p><b>2.2a</b></p>	<p>Correct method to find either <math>\overline{AB}</math> or <math>\overline{BA}</math></p> <p>cao</p> <p>Correct lengths for <math>OA</math> and <math>OB</math> (or their squares)</p> <p>Correct use of cosine rule for their <math>OA</math>, <math>OB</math> and <math>AB</math></p> <p><b>AG</b> – sufficient working must be shown</p>	<p><math>\cos AOB</math> may not be the subject, but substitutions must be correct for their values</p> <p>Condone this result from calculator without intermediate working.</p>
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Question			Answer	Marks	AO	Guidance
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7	(b)		$\sin^2 AOB = 1 - \left(-\frac{2\sqrt{5}}{25}\right)^2$ $\sin^2 AOB = \frac{121}{125} \Rightarrow \sin AOB = \frac{11\sqrt{5}}{25}$	M1  A1  [2]	3.1a  1.1	Using the identity $\cos^2 X + \sin^2 X = 1$ with $\cos X = -\frac{2\sqrt{5}}{25}$  Or exact equivalent – justification not required for taking the positive square root
7	(c)		$\text{Area of } OACB = 2 \left( \frac{1}{2} (\sqrt{20}) (5) \left( \frac{11\sqrt{5}}{25} \right) \right)$ 22	M1  A1 [2]	3.1a  1.1	Use of $A = ab \sin C$ (or equivalent) with $OA$ and $OB$ and $\sin AOB$  cao  May not use exact values here  Condone awrt 22.0