

Question		Answer	Marks	AO	Guidance	
12	(a)	Use $\frac{dy}{dx} = \frac{dy}{d\theta} \div \frac{d\theta}{dx}$ Obtain $\frac{-3\cos\theta}{2\sin\theta}$	M1 A1 [2]	1.1a 1.1		
12	(b)	$(y - 3\sin\theta) = \frac{-3\cos\theta}{2\sin\theta}(x - 2\cos\theta)$ $2y\sin\theta - 6\sin^2\theta = -3x\cos\theta + 6\cos^2\theta$ $2y\sin\theta + 3x\cos\theta = 6$ $12\sin\theta + 6\cos\theta = 6 \Rightarrow 2\sin\theta + \cos\theta = 1$	M1 M1 A1FT E1 [4]	3.1a 1.1 1.1 2.1	Attempt equation of straight line in any unsimplified form Accept x, y confusion Simplify their equation and use $\cos^2\theta + \sin^2\theta = 1$ Substitute (2, 6) and simplify to AG	OR M1 When $\theta = \theta_Q$, gradient of curve is given by $\frac{-3\cos\theta_Q}{2\sin\theta_Q}$ M1 The gradient of the line through (2, 6) and $(2\cos\theta_Q, 3\sin\theta_Q)$ is $\frac{3\sin\theta_Q - 6}{2\cos\theta_Q - 2}$ M1 Equate and clear fractions E1 Obtain AG
12	(c)	Use $R\sin(\theta + \alpha)$ on $2\sin\theta + \cos\theta$ $R\sin\alpha = 1, R\cos\alpha = 2$ Obtain $\alpha = 0.4636$ and $R = \sqrt{5}$ Use correct order of operations to solve $\sqrt{5}\sin(\theta + 0.4636) = 1$ Obtain 0 Obtain 2.21	M1 A1 M1 B1 A1 [5]	3.1a 1.1 1.1 2.2a 1.1	Should go as far as finding R and α Allow alternative forms Attempt to solve their $R\sin(\theta + \alpha)$ Or better (2.214345...)	OR M1 Square and use $\sin^2\theta + \cos^2\theta = 1$ A1 $4\sin^2\theta + 4\sin\theta(1 - 2\sin\theta) + (1 - \sin^2\theta) = 1$ M1 Simplify and solve $5\sin^2\theta - 4\sin\theta = 0$