| Question |     | on | Answer                                                                                          | Marks | AO           | Guidance                                         |                                                                                                                                                                                                                                                                           |
|----------|-----|----|-------------------------------------------------------------------------------------------------|-------|--------------|--------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 11       | (a) |    | $\int 1.\ln(x-4)dx$<br>so $u = \ln(x-4)$ and $v' = 1$                                           | M1    | <b>1.1</b> a | Attempt integration by parts, with correct parts | <i>u</i> and <i>v'</i> correctly allocated and correct<br>formula used<br>M0 if $v = x - 4$ from $v' = 1$                                                                                                                                                                 |
|          |     |    | $x\ln x-4  - \int \frac{x}{x-4} \mathrm{d}x$                                                    | A1    | 1.1          | Correct expression                               | Allow brackets not modulus<br>Allow $x \times \frac{1}{x-4}$ , even if subsequently spoilt                                                                                                                                                                                |
|          |     |    | $\int \frac{x}{x-4} dx = \int 1 + \frac{4}{x-4} dx$                                             | M1    | 3.1a         | Attempt to deal with improper fraction           | Allow sign error ie $1 - \frac{4}{x-4}$<br>Could use substitution of $u = x - 4$ but must<br>get as far as a proper fraction (ie $1 \pm 4u^{-1}$ )<br>Do not need to actually integrate for M1                                                                            |
|          |     |    | $= x + 4\ln\left x - 4\right $                                                                  | A1    | 1.1          | Correct integration of fraction                  | Allow brackets not modulus<br>Using a substitution gives $x - 4 + 4\ln x - 4 $ ;<br>must be in terms of x and not u for A1                                                                                                                                                |
|          |     |    | $\int \ln(x-4) dx$<br>= $x \ln  x-4  - x - 4 \ln  x-4  + c$<br>= $(x-4) \ln  x-4  - x + c$ A.G. | A1    | 2.4          | Show given answer with no errors seen            | Modulus required in final answer, as well as $+ c$<br>Can go from penultimate line in MS to given<br>answer with no further detail needed<br>Answer from using substitution will need to<br>justify changing $c \ge c + 4$ is a constant<br>hence $c'$ is also a constant |
|          |     |    |                                                                                                 | [5]   |              |                                                  | <b>NB</b> differentiating given answer is 0/5                                                                                                                                                                                                                             |

| Question |     | on | Answer                                                                                                     | Marks     | AO   | Guidance                                         |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |  |
|----------|-----|----|------------------------------------------------------------------------------------------------------------|-----------|------|--------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|
|          |     |    |                                                                                                            |           |      |                                                  | OR<br>B1 – use substitution of $v = x - 4$ , with<br>$\frac{dv}{dx} = 1$ seen, to obtain $\int \ln v dv$<br>if B0 as it is not explicit then next 4<br>marks are still available<br>M1 – attempt integration by parts on<br>$\int \ln v dv$ , using correct parts and<br>correct formula<br>A1 – obtain $v \ln  v  - v$ (allow no modulus )<br>A1 – obtain $(x - 4) \ln  x - 4  - (x - 4)$<br>A1 – obtain given answer, including<br>modulus sign, and with justification<br>for their <i>c</i> becoming <i>c'</i> |  |
|          | (b) | S  | State $x = 4$                                                                                              | B1<br>[1] | 2.2a |                                                  | Must be an equation                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                |  |
|          | (c) |    | $\int_{5}^{7} \ln(x-4) dx + \int_{4.5}^{5} \ln(x-4) dx$                                                    | M1        | 3.1a | Attempt sum of absolute areas                    | Or integral $\int_{5}^{7} \ln(x-4) dx - \int_{4.5}^{5} \ln(x-4) dx$                                                                                                                                                                                                                                                                                                                                                                                                                                                |  |
|          |     | 3  | $\ln 3 - 2 \int (\frac{1}{2} \ln \frac{1}{2} + \frac{1}{2})$ $\ln 3 - 2 - \frac{1}{2} \ln 2 + \frac{1}{2}$ | M1        | 3.1a | Attempt to rearrange to required form            | Use $\ln \frac{1}{2} = -\ln 2$ and gather like terms<br>Could follow M0<br>Allow M1 (implied) for $3\ln 3 + 0.5\ln 2 - 2.5$ ,<br>even if $-0.5\ln 0.5$ not seen first                                                                                                                                                                                                                                                                                                                                              |  |
|          |     | 3  | $\ln 3 - \frac{1}{2} \ln 2 - \frac{3}{2}$                                                                  | A1        | 1.1  | Obtain $3\ln 3 - \frac{1}{2}\ln 2 - \frac{3}{2}$ | Or $3\ln 3 - 0.5\ln 2 - 1.5$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       |  |