

The diagram shows a sector AOB of a circle with centre O and radius 6 cm.

The angle AOB is θ radians.

The area of the segment bounded by the chord AB and the arc AB is $7.2 \,\mathrm{cm}^2$.

(a) Show that
$$\theta = 0.4 + \sin \theta$$
. [3]

(b) Let $F(\theta) = 0.4 + \sin \theta$.

By considering the value of $F'(\theta)$ where $\theta = 1.2$, explain why using an iterative method based on the equation in part (a) will converge to the root, assuming that 1.2 is sufficiently close to the root.

(c) Use the iterative formula $\theta_{n+1} = 0.4 + \sin \theta_n$ with a starting value of 1.2 to find the value of θ correct to 4 significant figures.

You should show the result of each iteration.

(d) Use a change of sign method to show that the value of θ found in part (c) is correct to 4 significant figures. [3]