0	(a)	$0.25\{\sin 0 + \sin\left(\frac{1}{2}\sqrt{0.25}\right) + \sin\left(\frac{1}{2}\sqrt{0.5}\right)$ $+\sin\left(\frac{1}{2}\sqrt{0.75}\right)\}$	IVII	1,2	with height on left-hand side	Allow M1 if evaluated in degrees (0.00452)
		Lower bound = $0.253$	<b>A1</b>	1.1	Obtain 0.253, or better	soi as lower bound

Attempt four rectangles of width 0.25

No pood to soo sin()

**N/I1** 

Question		on	Answer	Marks	AO	Guidance	
			$0.25\{\sin(\frac{1}{2}\sqrt{0.25}) + \sin(\frac{1}{2}\sqrt{0.5}) + \sin(\frac{1}{2}\sqrt{0.75})\}$	M1	1.1a	Attempt rectangles of width 0.25, with	Or subtract sin0 from part (ii) and
						height on right-hand side	add sin0.5
			$+\sin\frac{1}{2}$				Allow M1 if evaluated in degrees
							(0.00670)
			H	A 1	1 1	Obt.: 0 272 - 0 274 (form one)	M0 if sin0 explicitly included
			Upper bound= 0.373 or 0.374	A1	1.1	Obtain 0.373 or 0.374 (from rounding upper bound up), or better	soi as upper bound
				[4]		upper bound up), or better	
	(b)	(i)	$t^2 = x - 1$	M1	2.1	Attempt to link $dt$ and $dx$	
	()	(-)	$ \begin{array}{c} t - x - 1 \\ 2t dt = dx \end{array} $	A1	2.1	Obtain correct equation linking dt and	$\frac{1}{2}$
			ztut - ux			dx	Allow for $dt = \frac{1}{2}(x-1)^{-\frac{1}{2}} dx$ oe
			$\int \sin\left(\frac{1}{2}\sqrt{x-1}\right) dx = \int \sin\left(\frac{1}{2}t\right) 2t dt$	A1	2.5	Attempt integrand in terms of <i>t</i> to	Award A1 once all elements are
			$\int \sin\left(\frac{1}{2}\sqrt{x-1}\right) dx = \int \sin\left(\frac{1}{2}t\right) 2t dt$ $= \int 2t \sin\left(\frac{1}{2}t\right) dt  \mathbf{A.G.}$			obtain given answer	correct, even if not in same order
			$= \int 2t \sin(\frac{1}{2}t) dt \ \mathbf{A.G.}$				as given answer
							BOD if no brackets
				[3]			
	<b>(b)</b>	(ii)	$-4t\cos\left(\frac{1}{2}t\right) + \int 4\cos\left(\frac{1}{2}t\right) dt$	M1*	3.1a	Attempt integration by parts	Correct parts
				A 4	2.1		As far as first stage
			$-4t\cos\left(\frac{1}{2}t\right) + 8\sin\left(\frac{1}{2}t\right)$	A1	2.1	Correct integral	
			$\left(-4\cos\frac{1}{2} + 8\sin\frac{1}{2}\right) - \left(-0 + 0\right)$	M1d*	2.1	Attempt use of limits	Using either $t$ or $x$ , but must be
			2 2				consistent
							Condone no clear use of the lower
							limit for M1
			$8\sin\frac{1}{2} - 4\cos\frac{1}{2}  \mathbf{AG}$	A1	2.4	Obtain given answer	Must see some indication that
				F 43			lower limit considered
				[4]			